

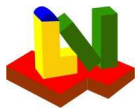
ASME BPVC VIII-1 2017
Example E4.4.7 - E4.4.8 PTB-4-2013

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Layout

Input values:	1.234	or	1.234
Calculated values:	1.234	or	1.234
Critical values:	1.234	or	1.234
Estimated values:	1.234	or	1.234



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Example E4.4.7 - E4.4.8 PTB-4-2013

Comparison - Form for equations

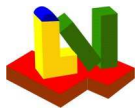
Equation form

Comment

Results for example E4.3.7-8 acc. ASME and Lauterbach Verfahrenstechnik GmbH (LV)
The LV-program uses formulas for thick cylinders acc. ASME VIII UG33 and App.1.

Equations

	Value
Conversion factor	$mm2in = 0.03937$
.	$mm^2toin^2 = 0.00155$
.	$mm^4toin^4 = 0.0000024027$
'Results Ex. E4.4.7 Large End LV and ASME	0
Del acc.to LV = #85(5)	1.836
Del acc. to Asme = 1.75	1.75
Required area acc. LV	$ArL = 0.00155 * \#103(5)$
Required area ASME	$ArLAsme = 1.5622$
Difference in %	$Diff1 = (ArL - ArLAsme) / ArLAsme * 100$
Required area acc. LV	$AeL = 0.00155 * \#105(5)$
Required area ASME	$AeLAsme = 32.1407$
Difference in %	$Diff2 = (AeL - AeLAsme) / AeLAsme * 100$
Required moment of inertia acc.LV	$IsL = 0.000002407 * \#76(4)$
Required moment of inertia acc.LV	$IsAsme = 81.845$
Difference in %	$Diff3 = (81.53 - 81.845) / 81.845 * 100$
'Results Ex. E4.4.7 Small End LV and ASME	0
Required area acc. LV	$ArS = 0.00155 * \#104(2)$
Required area ASME	$ArSAsme = 1.1106$
Difference in %	$Diff4 = (ArS - ArSAsme) / ArSAsme * 100$
Required area acc. LV	$Aes = 0.00155 * \#106(2)$
Required area ASME	$AesAsme = 10.1129$
Difference in %	$Diff5 = (Aes - AesAsme) / AesAsme * 100$
Required moment of inertia acc.LV	$IsS = 0.000002407 * \#76(7)$
Required moment of inertia acc.LV	$IsAsme = 16.7632$
Difference in %	$Diff6 = (16.79 - 16.7632) / 16.7632 * 100$
'Results Ex. E4.4.8 Large End LV and ASME	0
Required moment of inertia acc.LV	$Is = 0.000002407 * \#76(10)$
Required moment of inertia acc.LV	$IsAsme = 13.8199$
Difference in %	$Diff7 = (Is - IsAsme) / IsAsme * 100$
Required moment of inertia acc.LV	$I's = 0.000002407 * \#77(10)$
Required moment of inertia acc.LV	$I'sAsme = 17.7504$
Difference in %	$Diff7 = (I's - I'sAsme) / I'sAsme * 100$
'Maximum difference between LV and ASME	0
$Dmax = \text{Max}(Diff1 ; Diff2 ; Diff3 ; Diff4 ; Diff5 ; Diff6 ; Diff7)$	1.969



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Example E4.4.7 - E4.4.8 PTB-4-2013

E4.4.7 Large End - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition

Area at the wide end of a cone-cylinder-juncture without knuckle acc. App.1-8

Type of stiffener

No stiffener

External design pressure

p_D

14.7 psi

Hydrostatic head

D_p

0 psi

Calculation pressure

P_0

14.7 psi

Calculation temperature

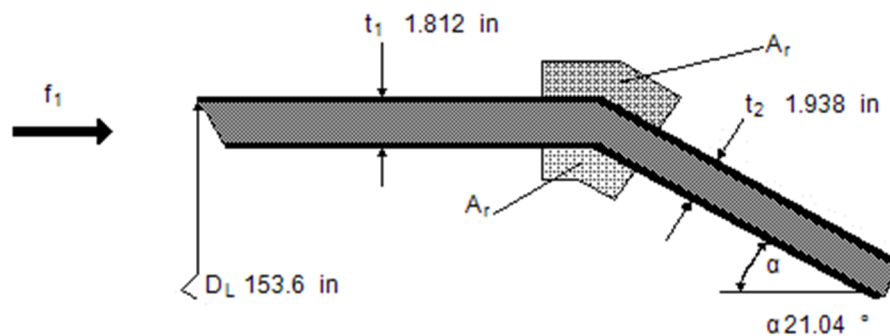
T_0

300 °F

Axial load (for positive tension)

f_1

497.1 lbf/in



Cylinder

Final wall thickness

t_1

1.812 in

Wall thickness allowance

c_1

0 in

Allowance (corrosion)

c_2

0.125 in

Final thickness without allowances

t_s

1.687 in

Outside diameter

D_L

153.6 in

Tip radius $(=D_L/2)$

R_L

76.8 in

Required thickness without allowances (UG-28)

t_{1r}

0.9549 in

Required thickness with allowances (UG-28)

t_{1r+}

1.08 in

Joint efficiency factor

E_1

1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

S_s

20015 psi

Modulus of elasticity

E_s

2.9e+7 psi

Cone

Final wall thickness

t_2

1.938 in

Wall thickness allowance

c_1

0 in

Allowance (corrosion)

c_2

0.125 in

Final thickness without allowances

t_c

1.813 in

Half apex angle $(\leq 60^\circ)$

α

21.04 °

Required thickness without allowances (UG-33)

t_{2r}

0.3639 in

Required thickness with allowances (UG-33)

t_{2r+}

0.4889 in

Joint efficiency factor

E_2

1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

S_c

20015 psi

Modulus of elasticity

E_c

2.9e+7 psi

Stiffening ring

Material K02700-SA-516-70-Class:-Size:

Actual cross section of the stiffener

A_r

34 in²

Allowable stress

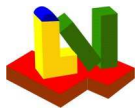
S_r

20015 psi

Modulus of elasticity

E_r

2.9e+7 psi



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Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Factor (≥ 1)	k	1
Ratio	$P_0/S_s E_1$	7.344e-4
Angle	D_{el}	1.836 °
Effective load	Q_L	1062 lbf/in
Cross sectional area	A_{rL}	1.565 in ²
Effective area	A_{eL}	32.14 in ²
Required cross section of reinforcement	A_{req}	0 in ²
Remark	Stiffening required acc. App. 1-8 (b)	

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

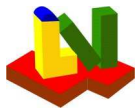
$$Q_L = P_0 \cdot \frac{R_L}{2} + f_1 = 1.014 \text{ bar} \cdot \frac{1951 \text{ mm}}{2} + 87.06 \text{ N/mm} = 185.9 \text{ N/mm}$$

$$A_{rL} = \frac{k \cdot Q_L \cdot R_L \cdot \tan(\alpha)}{S_s \cdot E_1} \cdot \left(1 - \frac{P_0 \cdot R_L - Q_L}{4 \cdot Q_L} \cdot \frac{D_{el}}{\alpha} \right) =$$

$$\frac{1 \cdot 185.9 \text{ N/mm} \cdot 1951 \text{ mm} \cdot 0.3846}{138 \text{ N/mm}^2 \cdot 1} \cdot \left(1 - \frac{1.014 \text{ bar} \cdot 1951 \text{ mm} - 185.9 \text{ N/mm}}{4 \cdot 185.9 \text{ N/mm}} \cdot \frac{1.836^\circ}{21.04^\circ} \right) = 1010 \text{ mm}^2 \quad (1)$$

$$A_{eL} = 0.55 \cdot \sqrt{(D_L \cdot t_s)} \cdot \left(\frac{t_s + t_c}{\cos(\alpha)} \right) =$$

$$0.55 \cdot \sqrt{(3902 \text{ mm} \cdot 42.86 \text{ mm})} \cdot \left(\frac{42.86 \text{ mm} + 46.04 \text{ mm}}{0.9333} \right) = 20736 \text{ mm}^2 \quad (2)$$



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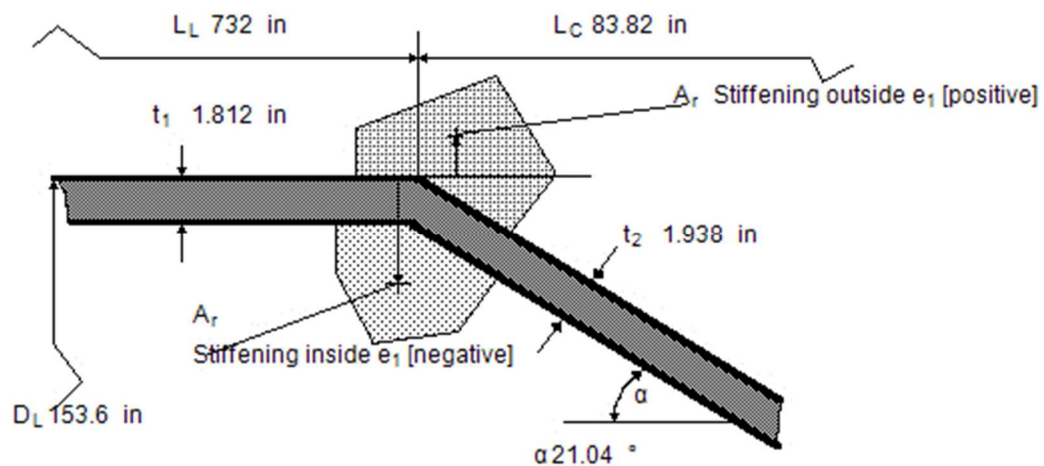
Example E4.4.7 - E4.4.8 PTB-4-2013

E4.4.7 Large End/Line-of-support - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition

Moment of inertia at the wide end of a cone-cylinder-juncture under external pressure acc. App. 1-8

(Line-of-support)

External design pressure	p_D	14.7 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	14.7 psi
Calculation temperature	T_0	300 °F
Axial load (for positive tension)	f_1	497.1 lbf/in



Cylinder

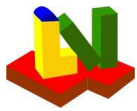
Design wall thickness	t_1	1.812 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_s	1.687 in
Required thickness without allowances (UG-28)	t_{1r}	0.9549 in
Required thickness with allowances (UG-28)	t_{1r+}	1.08 in
Outside diameter	D_L	153.6 in
Tip radius	R_L	76.81 in
Buckling length	L_L	732 in

Cone

Design wall thickness	t_2	1.938 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_c	1.813 in
Required thickness without allowances (UG-33)	t_{2r}	0.3639 in
Required thickness with allowances (UG-33)	t_{2r+}	0.4889 in
Half apex angle ($\leq 60^\circ$)	α	21.04 °
Buckling length	L_C	83.82 in

Stiffening ring

Material	K02700-SA-516-70-Class:-Size:	
Spec. Min. Yield	S_y	2.9e+7 psi
Applicable material chart	Fig	CS-2
Centroidal distance	e_1	in
Cross sectional area	A_r	0 in ²
Moment of inertia	I_r	in ⁴



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Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Equivalent length	M	393.8 in
Effective load	F_L	5980 lbf/in
Reference area	A_{TL}	693.6 in ²
Factor	B	993.4 psi
Factor (see material chart)	A	6.96e-5
Required moment of inertia	I_s	81.38 in ⁴
Required moment of inertia	I'_s	104.5 in ⁴
Length of support	$0.55 \cdot \sqrt{(D \cdot t_s)}$	8.856 in
Available moment of inertia	I'	in ⁴

Remark

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$R_s = R_L - L_C \cdot \sin(\alpha) = 1951 \text{ mm} - 2129 \text{ mm} \cdot 0.359 = 1172 \text{ mm}$$

$$M = \frac{-R_L \cdot \tan(\alpha)}{2} + \frac{L_L}{2} + \frac{R_L^2 - R_s^2}{3 \cdot R_L \cdot \tan(\alpha)} =$$

$$\frac{-1951 \text{ mm} \cdot 0.3846}{2} + \frac{18593 \text{ mm}}{2} + \frac{(1951 \text{ mm})^2 - (1172 \text{ mm})^2}{3 \cdot 1951 \text{ mm} \cdot 0.3846} = 10002 \text{ mm}$$

App. 1-8 b-3) Step 1

$$F_L = P_0 \cdot M + f_1 \cdot \tan(\alpha) =$$

$$1.014 \text{ bar} \cdot 10002 \text{ mm} + 87.06 \text{ N/mm} \cdot 0.3846 = 1047 \text{ N/mm}$$

App. 1-8 b-3) Step 1

$$A_{TL} = L_L \cdot \frac{t_s}{2} + L_C \cdot \frac{t_c}{2} + A_s =$$

$$18593 \text{ mm} \cdot \frac{42.86 \text{ mm}}{2} + 2129 \text{ mm} \cdot \frac{46.04 \text{ mm}}{2} + 0 \text{ mm}^2 = 447474 \text{ mm}^2$$

App. 1-8 a)

$$B = \frac{3}{4} \cdot \frac{F_L \cdot D_L}{A_{TL}} = \frac{3}{4} \cdot \frac{1047 \text{ N/mm} \cdot 3902 \text{ mm}}{447474 \text{ mm}^2} = 6.849 \text{ N/mm}^2$$

App. 1-8 b-3) Step 1

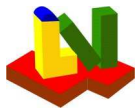
$$I_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{14} = 6.96e-5 \cdot (3902 \text{ mm})^2 \cdot \frac{447474 \text{ mm}^2}{14} = 3.387e+7 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$I'_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{10.9} = 6.96e-5 \cdot (3902 \text{ mm})^2 \cdot \frac{447474 \text{ mm}^2}{10.9} = 4.35e+7 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$0.55 \cdot \sqrt{(D \cdot t_s)} = 0.55 \cdot \sqrt{(3902 \text{ mm} \cdot 42.86 \text{ mm})} = 224.9 \text{ mm}$$



ASME BPVC VIII-1 2017

Example E4.4.7 - E4.4.8 PTB-4-2013

E4.4.7 Small End - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition

Area at the small end of a cone-cylinder-juncture without knuckle

Type of stiffener

No stiffener

External design pressure

p_D

14.7 psi

Hydrostatic head

D_p

0 psi

Calculation pressure

p_0

14.7 psi

Calculation temperature

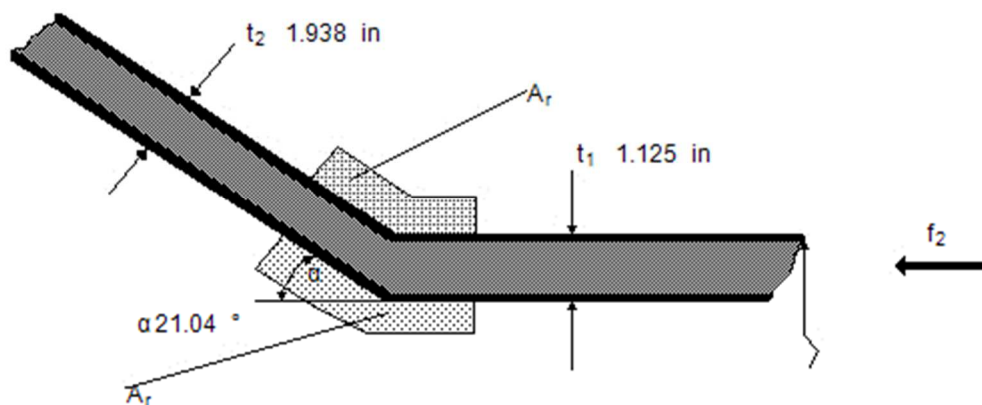
T_0

300 °F

Axial load (for positive tension)

f_2

913 lbf/in



Cylinder

Final wall thickness

t_1

1.125 in

Wall thickness allowance

c_1

0 in

Allowance (corrosion)

c_2

0.125 in

Final thickness without allowances

t_s

1 in

Outside diameter

D_S

92.25 in

Tip radius $(=D_S/2)$

R_S

46.12 in

Required thickness without allowances (UG-28)

t_{1r}

0.6718 in

Required thickness with allowances (UG-28)

t_{1r+}

0.7968 in

Joint efficiency factor

E_1

1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

S_s

20015 psi

Modulus of elasticity

E_s

2.9e+7 psi

Cone

Final wall thickness

t_2

1.938 in

Wall thickness allowance

c_1

0 in

Allowance (corrosion)

c_2

0.125 in

Final thickness without allowances

t_c

1.813 in

Semi aperture angle $(\leq 60^\circ)$

α

21.04 °

Required thickness without allowances (UG-33)

t_{2r}

0.3639 in

Required thickness with allowances (UG-33)

t_{2r+}

0.4889 in

Joint efficiency factor

E_2

1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

S_c

20015 psi

Modulus of elasticity

E_c

2.9e+7 psi

Stiffening ring

Material

Actual cross section of the stiffener

A_r

in²

Allowable stress

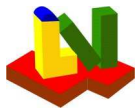
S_r

psi

Modulus of elasticity

E_r

psi



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Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Factor	k	1 ≥ 1
Effective load	Q_S	1252 lbf/in
Cross sectional area	A_{rS}	1.11 in ²
Effective area	A_{eS}	9.936 in ²
Required cross section of the stiffener	A_{req}	0 in ²
Remark		

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

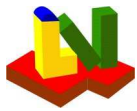
$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$Q_S = P_0 \cdot \frac{R_S}{2} + f_2 = 1.014 \text{ bar} \cdot \frac{1172 \text{ mm}}{2} + 159.9 \text{ N/mm} = 219.3 \text{ N/mm}$$

$$A_{rS} = \frac{k \cdot Q_S \cdot R_S \cdot \tan(\alpha)}{S_s \cdot E_1} = \frac{1 \cdot 219.3 \text{ N/mm} \cdot 1172 \text{ mm} \cdot 0.3846}{138 \text{ N/mm}^2 \cdot 1} = 716 \text{ mm}^2 \quad (3)$$

$$A_{eS} = 0.55 \cdot \sqrt{D_S \cdot t_s} \cdot \left[\frac{t_s - t + (t_c - t_r)}{\cos(\alpha)} \right] =$$

$$0.55 \cdot \sqrt{2343 \text{ mm} \cdot 25.4 \text{ mm}} \cdot \left[\frac{25.4 \text{ mm} - 17.06 \text{ mm} + (46.05 \text{ mm} - 9.242 \text{ mm})}{0.9333} \right] = 6410 \text{ mm}^2 \quad (4)$$



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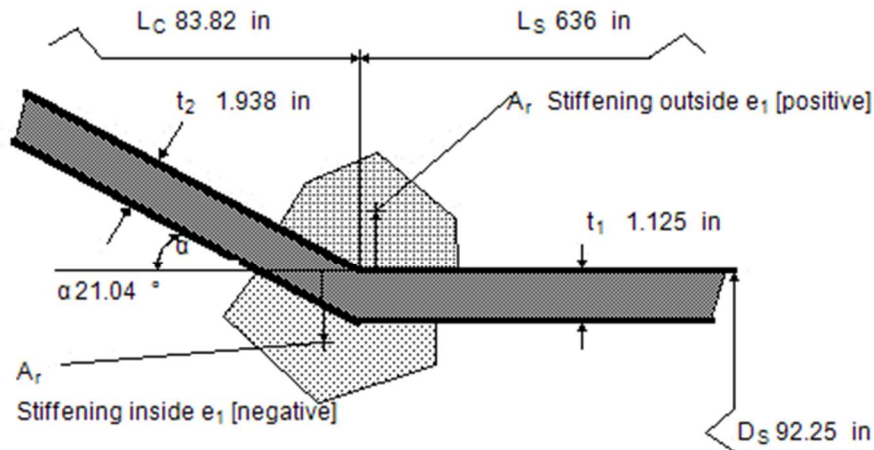
Example E4.4.7 - E4.4.8 PTB-4-2013

E4.4.7 Small End/Line-of-support - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition

Moment of inertia at the small end of a cone-cylinder-juncture under external pressure acc. App.1-8

(Line-of-support)

External design pressure	p_D	14.7 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	14.7 psi
Calculation temperature	T_0	300 °F
Axial load (for positive tension)	f_2	913 lbf/in



Cylinder

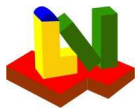
Final wall thickness	t_1	1.125 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_s	1 in
Required thickness without allowances (UG-28)	t_{1r}	0.6718 in
Required thickness with allowances (UG-28)	t_{1r+}	0.7968 in
Outside diameter	D_S	92.25 in
Tip radius ($=D_S/2$)	R_S	46.12 in
Buckling length	L_S	636 in

Cone

Final wall thickness	t_2	1.938 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_c	1.813 in
Required thickness without allowances (UG-33)	t_{2r}	0.3639 in
Required thickness with allowances (UG-33)	t_{2r+}	0.4889 in
Semi-apex angle ($\leq 60^\circ$)	α	21.04 °
Buckling length	L_C	83.82 in

Stiffening ring

Material	K02700-SA-516-70-Class:-Size:	
Spec. Min. Yield	S_y	2.9e+7 psi
Applicable material chart	Fig	CS-2
Centroidal distance	e_r	in
Cross sectional area	A_r	0 in ²
Moment of inertia	I_r	in ⁴



ASME BPVC VIII-1 2017

Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Equivalent length	N	362.3 in
Effective load	F_S	5677 lbf/in
Reference area	A_{TS}	394 in ²
Factor	B	997 psi
Factor (see material chart)	A	6.998e-5
Required moment of inertia	I_s	16.76 in ⁴
Required moment of inertia	I'_s	21.53 in ⁴
Length of support	$0.55 \cdot \sqrt{(D \cdot t_s)}$	5.283 in
Available moment of inertia	I'	in ⁴

Remark

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$R_s = R_L - L_C \cdot \sin(\alpha) = 1952 \text{ mm} - 2129 \text{ mm} \cdot 0.359 = 1172 \text{ mm}$$

$$N = \frac{R_s \cdot \tan(\alpha)}{2} + \frac{L_s}{2} + \frac{RL^2 - RS^2}{6 \cdot R_s \cdot \tan(\alpha)} =$$

$$\frac{1172 \text{ mm} \cdot 0.3846}{2} + \frac{16154 \text{ mm}}{2} + \frac{(1952 \text{ mm})^2 - (1172 \text{ mm})^2}{6 \cdot 1172 \text{ mm} \cdot 0.3846} = 9203 \text{ mm}$$

$$994.3 \text{ N/mm} = 1.014 \text{ bar} \cdot 9203 \text{ mm} + 159.9 \text{ N/mm} \cdot 0.3846$$

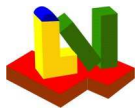
$$A_{TS} = L_s \cdot \frac{t_s}{2} + L_C \cdot \frac{t_c}{2} + A_s = 16154 \text{ mm} \cdot \frac{25.4 \text{ mm}}{2} + 2129 \text{ mm} \cdot \frac{46.05 \text{ mm}}{2} + 0 \text{ mm}^2 = 254182 \text{ mm}^2$$

$$B = \frac{3}{4} \cdot \frac{F_s \cdot D_s}{A_{TS}} = \frac{3}{4} \cdot \frac{994.3 \text{ N/mm} \cdot 2343 \text{ mm}}{254182 \text{ mm}^2} = 6.874 \text{ N/mm}^2$$

$$I_s = \frac{A \cdot DS^2 \cdot A_{TS}}{14} = \frac{6.998e-5 \cdot (2343 \text{ mm})^2 \cdot 254182 \text{ mm}^2}{14} = 6975754 \text{ mm}^4$$

$$I'_s = \frac{A \cdot DS^2 \cdot A_{TS}}{10.9} = \frac{6.998e-5 \cdot (2343 \text{ mm})^2 \cdot 254182 \text{ mm}^2}{10.9} = 8959684 \text{ mm}^4$$

$$0.55 \cdot \sqrt{(D \cdot t_s)} = 0.55 \cdot \sqrt{(D \cdot 25.4 \text{ mm})} = 134.2 \text{ mm}$$



ASME BPVC VIII-1 2017
Example E4.4.7 - E4.4.8 PTB-4-2013

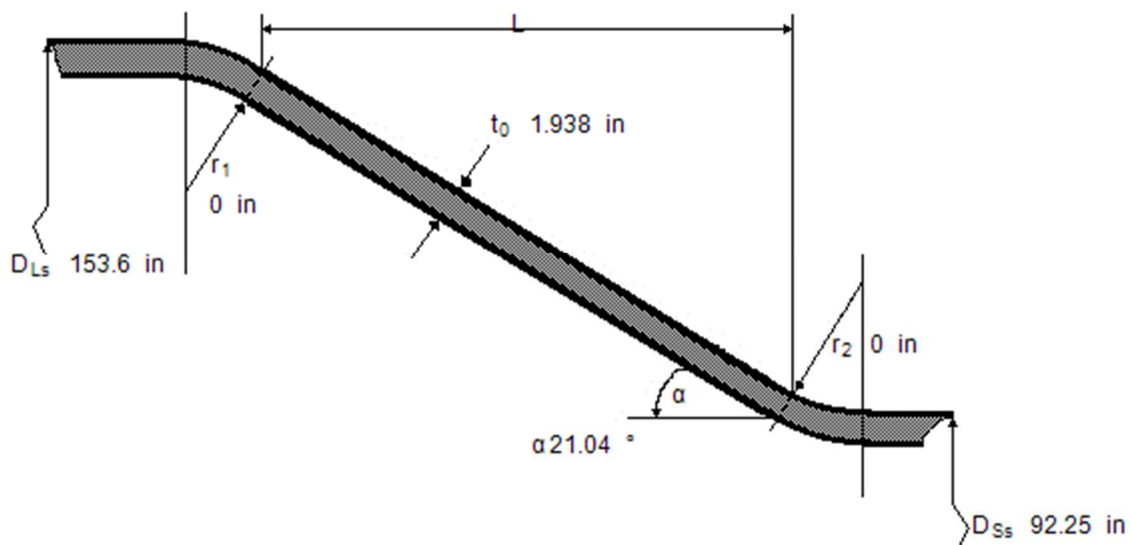
E4.4.8 Large and Small End - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition

Conical shells under external pressure acc. UG-33(f)

External design pressure	p_D	14.7 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	14.7 psi
Calculation temperature	T_0	300 °F

Material K02700-SA-516-70-Class:-Size:

Spec. Min. Yield	S_y	37710 psi
Allowable stress	S_0	20015 psi
Applicable material chart	Fig	CS-2
E-Modulus	E	2.9e+7 psi

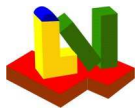


Cone wall thickness with allowances	t_0	1.938 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Cone wall thickness without allowances	t	1.813 in

Is a cylinder connected, which does not act as line of support?

	N	(Y/N)
Outside diameter (wide end)	D_{Ls}	153.6 in
Knuckle radius (wide end)	r_1	0 in
Outside diameter (small end)	D_{Ss}	92.25 in
Knuckle radius (small end)	r_2	0 in
Half apex angle ($\leq 60^\circ$)	α	21.04 °

Proof for cross-section area according to App. 1-8 required for cone-connection without knuckle



ASME BPVC VIII-1 2017

Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Effective thickness	$t_e = t \cdot \cos(\alpha)$	t_e	1.692 in
Axial length of the cone		L	79.79 in
Design length		L_e	63.85 in
Ratio		L_e/D_L	0.4156
Ratio		D_L/t_e	90.81
Factor according to fig. 5-UGO-28.0		A	0.004054
Factor (see material chart)		B	16850 psi
Factor	$2 \cdot \min(S_0; 9 \cdot B)$	S	31589 psi
Allowable external pressure (for t_0)		P	247.4 psi
Allowable pressure without hydrostatic head		MEP	247.4 psi
Required thickness (for P_0)		t	0.3664 in
Required thickness incl. allowances		$t+c_1+c_2$	0.4914 in

Remark

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$D_L = D_{Ls} - r_1 \cdot (1 - \cos(\alpha)) = 3902 \text{ mm} - 0 \text{ mm} \cdot (1 - 0.9333) = 3902 \text{ mm}$$

$$D_S = D_{Ss} + r_2 \cdot (1 - \cos(\alpha)) = 2343 \text{ mm} + 0 \text{ mm} \cdot (1 - 0.9333) = 2343 \text{ mm}$$

$$L = \frac{(D_L - D_S)}{2} \cdot \tan(\alpha) = \frac{(3902 \text{ mm} - 2343 \text{ mm})}{2} \cdot 0.3846 = 2027 \text{ mm}$$

$$L_1 = r_1 \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.359 = 0 \text{ mm}$$

$$L_2 = r_2 \cdot \left(\frac{D_{Ss}}{D_{Ls}} \right) \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.6005 \cdot 0.359 = 0 \text{ mm}$$

$$L_3 = \frac{L}{2} \cdot \frac{(D_L + D_S)}{D_{Ls}} = \frac{2027 \text{ mm}}{2} \cdot \frac{(3902 \text{ mm} + 2343 \text{ mm})}{3902 \text{ mm}} = 1622 \text{ mm}$$

$$L_e = L_1 + L_2 + L_3 = 0 \text{ mm} + 0 \text{ mm} + 1622 \text{ mm} = 1622 \text{ mm}$$

1) for $D_L/t_0 \geq 10$

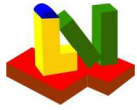
$$Pa(B) = \frac{4 \cdot B}{3 \cdot \left(\frac{D_L}{t_0} \right)} = \frac{4 \cdot 116.2 \text{ N/mm}^2}{3 \cdot 90.81} = 1.706 \text{ N/mm}^2$$

UG-33 f-a) Step 6

$$Pa(E) = \frac{2 \cdot A \cdot E}{3 \cdot \left(\frac{D_L}{t_0} \right)} = \frac{2 \cdot 0.004054 \cdot 199948 \text{ N/mm}^2}{3 \cdot 90.81} = 5.951 \text{ N/mm}^2$$

UG-33 f-a) Step 7

2) for $D_L/t_0 < 10$



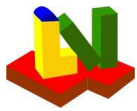
ASME BPVC VIII-1 2017
Example E4.4.7 - E4.4.8 PTB-4-2013

$$P_{a1} = \left[\frac{2.167}{\frac{D_L}{t_0}} - 0.0833 \right] \cdot B = \left[\frac{2.167}{90.81} - 0.0833 \right] \cdot 116.2 \text{ N/mm}^2 = -6.905 \text{ N/mm}^2$$

UG-33 f-b) Step 2

$$P_{a2} = \frac{2 \cdot S}{\frac{D_L}{t_0}} \cdot \left[1 - \frac{2 \cdot S}{\frac{D_L}{t_0}} \right] = \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \cdot \left[1 - \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \right] = 4.744 \text{ N/mm}^2$$

UG-33 f-b) Step 3



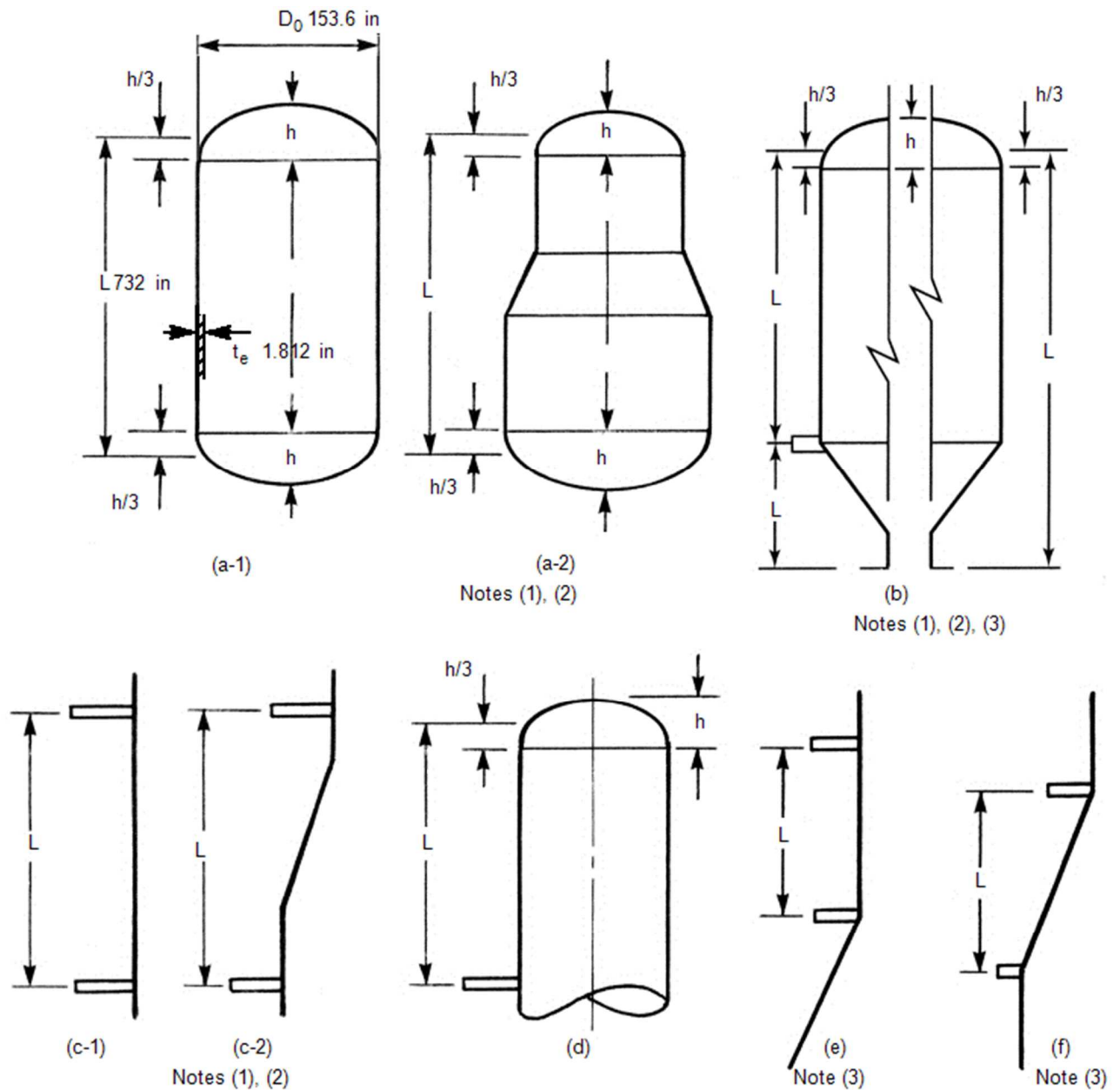
ASME BPVC VIII-1 2017
Example E4.4.7 - E4.4.8 PTB-4-2013

Thickness of shells and tubes under external pressure ASME BPVC VIII UG-28 and Appendix I, 2017 Edition

Cylindrical shells under external pressure

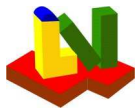
External design pressure
Hydrostatic head
External calculation pressure
Calculation temperature

p_D 14.7 psi
 D_p 0 psi
 p_0 14.7 psi
 T_0 300 °F



Outside diameter
Design wall thickness
Wall thickness allowance
Allowance (corrosion)
Buckling length

D_0 153.6 in
 t_e 1.812 in
 c_1 0 in
 c_2 0.125 in
 L 732 in



ASME BPVC VIII-1 2017

Example E4.4.7 - E4.4.8 PTB-4-2013

Material K02700-SA-516-70-Class:-Size:

Spec. Min. Yield	S_y	37710 psi
Allowable stress	S_0	20015 psi
Applicable material chart	Fig	CS-2
Modulus of elasticity	E	2.829e+7 psi

Results

Effective thickness	t_0	1.687 in
Ratio	L/D_0	4.765
Ratio	D_0/t_0	91.03
Factor according to ASME-IID\Table G	A	2.883e-4
Factor (see material chart)	B	4141 psi
Factor $2 \cdot \text{Min}(S_0; 9 \cdot B)$	S	7454 psi
Required thickness acc. UG-28	t_{UG-28}	24.25 mm
Required thickness acc. UG-16	t_{UG-16}	1.5 mm
Required thickness	t	0.9549 in
Required thickness incl. allowances	$t+c_1+c_2$	1.08 in
Allowable excess pressure	P	59.74 psi
Allowable pressure without hydrostatic head	MAWP	59.74 psi

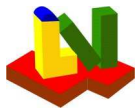
Remark

Equations

$$\frac{D_0}{t_0} \geq 10 \Leftrightarrow 91.03 \geq 10 \quad \text{UG-28 c) (1)}$$

$$Pa(B) = \frac{4 \cdot B}{3 \cdot \frac{D_0}{t_0}} = \frac{4 \cdot 28.55 \text{ N/mm}^2}{3 \cdot 91.03} = 0.4182 \text{ MPa} \quad \text{Step 6}$$

$$Pa(E) = \frac{2 \cdot A \cdot E}{3 \cdot \frac{D_0}{t_0}} = \frac{2 \cdot 2.883e-4 \cdot 195067 \text{ N/mm}^2}{3 \cdot 91.03} = 0.4119 \text{ MPa} \quad \text{Step 7}$$



ASME BPVC VIII-1 2017 **Example E4.4.7 - E4.4.8 PTB-4-2013**

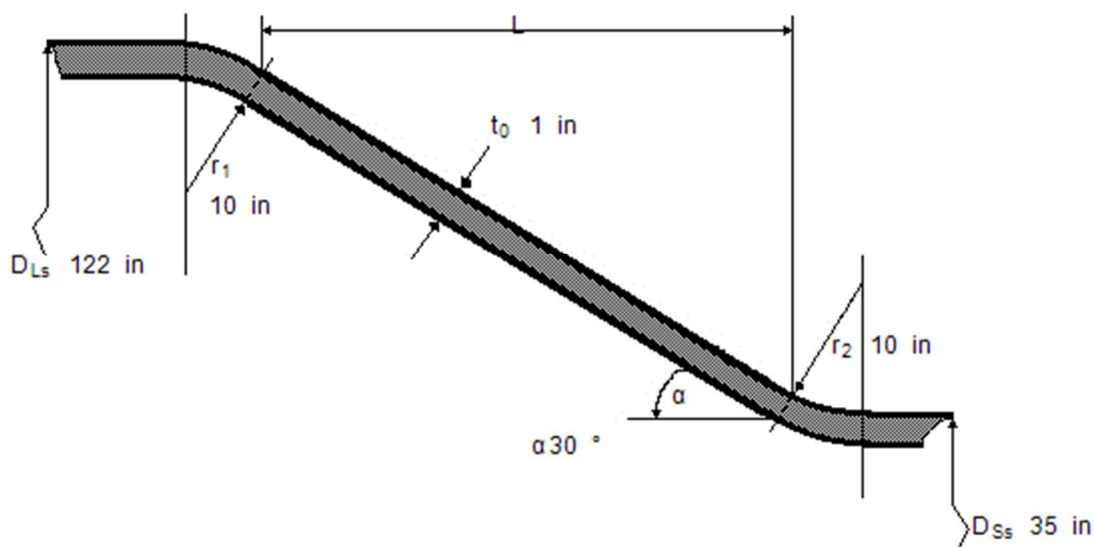
Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition

Conical shells under external pressure acc. UG-33(f)

External design pressure	p_D	19.53 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	19.53 psi
Calculation temperature	T_0	300 °F

Material K02700-SA-516-70-Class:-Size:

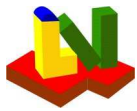
Spec. Min. Yield	S_y	37710 psi
Allowable stress	S_0	20015 psi
Applicable material chart	Fig	CS-2
E-Modulus	E	2.9e+7 psi



Cone wall thickness with allowances	t_0	1 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0 in
Cone wall thickness without allowances	t	1 in

Is a cylinder connected, which does not act as line of support?

Outside diameter (wide end)	D_{Ls}	122 in
Knuckle radius (wide end)	r_1	10 in
Outside diameter (small end)	D_{Ss}	35 in
Knuckle radius (small end)	r_2	10 in
Half apex angle ($\leq 60^\circ$)	α	30 °



ASME BPVC VIII-1 2017

Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Effective thickness	$t_e = t \cdot \cos(\alpha)$	t_e	0.866 in
Axial length of the cone		L	73.02 in
Design length		L_e	53.42 in
Ratio		L_e/D_L	0.4427
Ratio		D_L/t_e	139.3
Factor according to fig. 5-UGO-28.0		A	0.001947
Factor (see material chart)		B	14826 psi
Factor	$2 \cdot \min(S_0; 9 \cdot B)$	S	31589 psi
Allowable external pressure (for t_0)		P	141.9 psi
Allowable pressure without hydrostatic head		MEP	141.9 psi
Required thickness (for P_0)		t	0.3558 in
Required thickness incl. allowances		$t+c_1+c_2$	0.3558 in

Remark

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(30^\circ) = 0.866$$

$$\sin(\alpha) = \sin(\alpha) = \sin(30^\circ) = 0.5$$

$$\tan(\alpha) = \tan(\alpha) = \tan(30^\circ) = 0.5774$$

$$D_L = D_{Ls} - r_1 \cdot (1 - \cos(\alpha)) = 3099 \text{ mm} - 254 \text{ mm} \cdot (1 - 0.866) = 3065 \text{ mm}$$

$$D_S = D_{Ss} + r_2 \cdot (1 - \cos(\alpha)) = 889 \text{ mm} + 254 \text{ mm} \cdot (1 - 0.866) = 923 \text{ mm}$$

$$L = \frac{(D_L - D_S)}{2} \cdot \tan(\alpha) = \frac{(3065 \text{ mm} - 923 \text{ mm})}{2} \cdot 0.5774 = 1855 \text{ mm}$$

$$L_1 = r_1 \cdot \sin(\alpha) = 254 \text{ mm} \cdot 0.5 = 127 \text{ mm}$$

$$L_2 = r_2 \cdot \left(\frac{D_{Ss}}{D_{Ls}} \right) \cdot \sin(\alpha) = 254 \text{ mm} \cdot 0.2869 \cdot 0.5 = 36.43 \text{ mm}$$

$$L_3 = \frac{L}{2} \cdot \frac{(D_L + D_S)}{D_{Ls}} = \frac{1855 \text{ mm}}{2} \cdot \frac{(3065 \text{ mm} + 923 \text{ mm})}{3099 \text{ mm}} = 1193 \text{ mm}$$

$$L_e = L_1 + L_2 + L_3 = 127 \text{ mm} + 36.43 \text{ mm} + 1193 \text{ mm} = 1357 \text{ mm}$$

1) for $D_L/t_0 \geq 10$

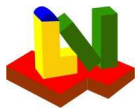
$$Pa(B) = \frac{4 \cdot B}{3 \cdot \left(\frac{D_L}{t_0} \right)} = \frac{4 \cdot 102.2 \text{ N/mm}^2}{3 \cdot 139.3} = 0.9783 \text{ N/mm}^2$$

UG-33 f-a) Step 6

$$Pa(E) = \frac{2 \cdot A \cdot E}{3 \cdot \left(\frac{D_L}{t_0} \right)} = \frac{2 \cdot 0.001947 \cdot 199948 \text{ N/mm}^2}{3 \cdot 139.3} = 1.862 \text{ N/mm}^2$$

UG-33 f-a) Step 7

2) for $D_L/t_0 < 10$



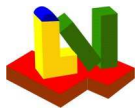
ASME BPVC VIII-1 2017
Example E4.4.7 - E4.4.8 PTB-4-2013

$$P_{a1} = \left[\frac{2.167}{\frac{D_L}{t_0}} - 0.0833 \right] \cdot B = \left[\frac{2.167}{139.3} - 0.0833 \right] \cdot 102.2 \text{ N/mm}^2 = -6.925 \text{ N/mm}^2$$

UG-33 f-b) Step 2

$$P_{a2} = \frac{2 \cdot S}{\frac{D_L}{t_0}} \cdot \left[1 - \frac{2 \cdot S}{\frac{D_L}{t_0}} \right] = \frac{2 \cdot 217.8 \text{ N/mm}^2}{139.3} \cdot \left[1 - \frac{2 \cdot 217.8 \text{ N/mm}^2}{139.3} \right] = 3.104 \text{ N/mm}^2$$

UG-33 f-b) Step 3



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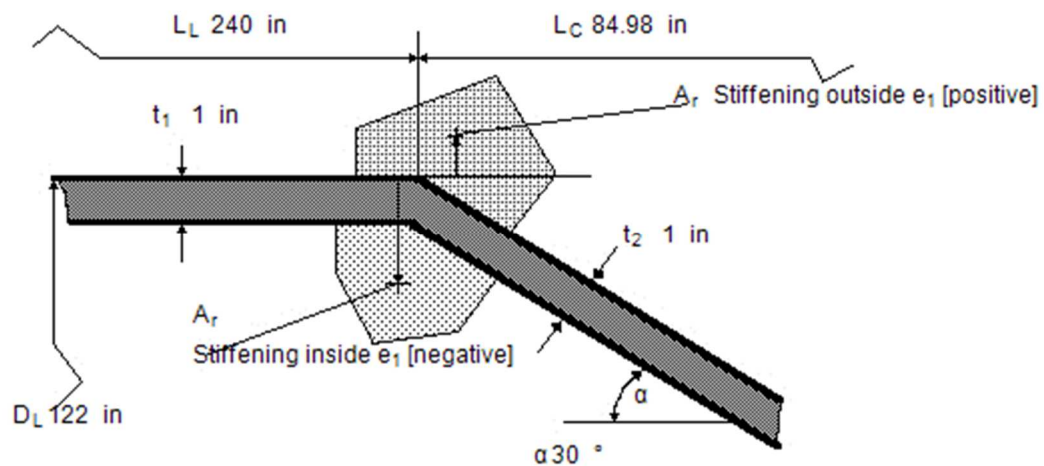
Example E4.4.7 - E4.4.8 PTB-4-2013

E4.4.8 Large End/Line-of-support - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition

Moment of inertia at the wide end of a cone-cylinder-juncture under external pressure acc. App. 1-8

(Line-of-support)

External design pressure	p_D	14.7 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	14.7 psi
Calculation temperature	T_0	300 °F
Axial load (for positive tension)	f_1	145 lbf/in



Cylinder

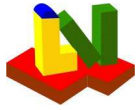
Design wall thickness	t_1	1 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0 in
Final thickness without allowances	t_s	1 in
Required thickness without allowances (UG-28)	t_{1r}	0.5205 in
Required thickness with allowances (UG-28)	t_{1r+}	0.5205 in
Outside diameter	D_L	122 in
Tip radius	R_L	61 in
Buckling length	L_L	240 in

Cone

Design wall thickness	t_2	1 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0 in
Final thickness without allowances	t_c	1 in
Required thickness without allowances (UG-33)	t_{2r}	0.3358 in
Required thickness with allowances (UG-33)	t_{2r+}	0.3358 in
Half apex angle ($\leq 60^\circ$)	α	30 °
Buckling length	L_C	84.98 in

Stiffening ring

Material	K02700-SA-516-70-Class:-Size:	
Spec. Min. Yield	S_y	2.9e+7 psi
Applicable material chart	Fig	CS-2
Centroidal distance	e_1	in
Cross sectional area	A_r	0 in ²
Moment of inertia	I_r	in ⁴



ASME BPVC VIII-1 2017

Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Equivalent length	M	134.7 in
Effective load	F_L	2064 lbf/in
Reference area	A_{TL}	162.5 in ²
Factor	B	1162 psi
Factor (see material chart)	A	8.142e-5
Required moment of inertia	I_s	14.07 in ⁴
Required moment of inertia	I'_s	18.07 in ⁴
Length of support	$0.55 \cdot \sqrt{(D \cdot t_s)}$	6.075 in
Available moment of inertia	I'	in ⁴
Remark	Stiffening required	

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(30^\circ) = 0.866$$

$$\sin(\alpha) = \sin(\alpha) = \sin(30^\circ) = 0.5$$

$$\tan(\alpha) = \tan(\alpha) = \tan(30^\circ) = 0.5774$$

$$R_s = R_L - L_C \cdot \sin(\alpha) = 1549 \text{ mm} - 2158 \text{ mm} \cdot 0.5 = 445 \text{ mm}$$

$$M = \frac{-R_L \cdot \tan(\alpha)}{2} + \frac{L_L}{2} + \frac{R_L^2 - R_S^2}{3 \cdot R_L \cdot \tan(\alpha)} =$$

$$\frac{-1549 \text{ mm} \cdot 0.5774}{2} + \frac{6096 \text{ mm}}{2} + \frac{(1549 \text{ mm})^2 - (445 \text{ mm})^2}{3 \cdot 1549 \text{ mm} \cdot 0.5774} = 3421 \text{ mm}$$

App. 1-8 b-3) Step 1

$$F_L = P_0 \cdot M + f_1 \cdot \tan(\alpha) =$$

$$1.014 \text{ bar} \cdot 3421 \text{ mm} + 25.39 \text{ N/mm} \cdot 0.5774 = 361.4 \text{ N/mm}$$

App. 1-8 b-3) Step 1

$$A_{TL} = L_L \cdot \frac{t_s}{2} + L_C \cdot \frac{t_c}{2} + A_s =$$

$$6096 \text{ mm} \cdot \frac{25.4 \text{ mm}}{2} + 2158 \text{ mm} \cdot \frac{25.4 \text{ mm}}{2} + 0 \text{ mm}^2 = 104831 \text{ mm}^2$$

App. 1-8 a)

$$B = \frac{3}{4} \cdot \frac{F_L \cdot D_L}{A_{TL}} = \frac{3}{4} \cdot \frac{361.4 \text{ N/mm} \cdot 3099 \text{ mm}}{104831 \text{ mm}^2} = 8.013 \text{ N/mm}^2$$

App. 1-8 b-3) Step 1

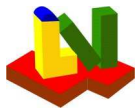
$$I_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{14} = 8.142e-5 \cdot (3099 \text{ mm})^2 \cdot \frac{104831 \text{ mm}^2}{14} = 5854591 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$I'_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{10.9} = 8.142e-5 \cdot (3099 \text{ mm})^2 \cdot \frac{104831 \text{ mm}^2}{10.9} = 7519658 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$0.55 \cdot \sqrt{(D \cdot t_s)} = 0.55 \cdot \sqrt{(3099 \text{ mm} \cdot 25.4 \text{ mm})} = 154.3 \text{ mm}$$



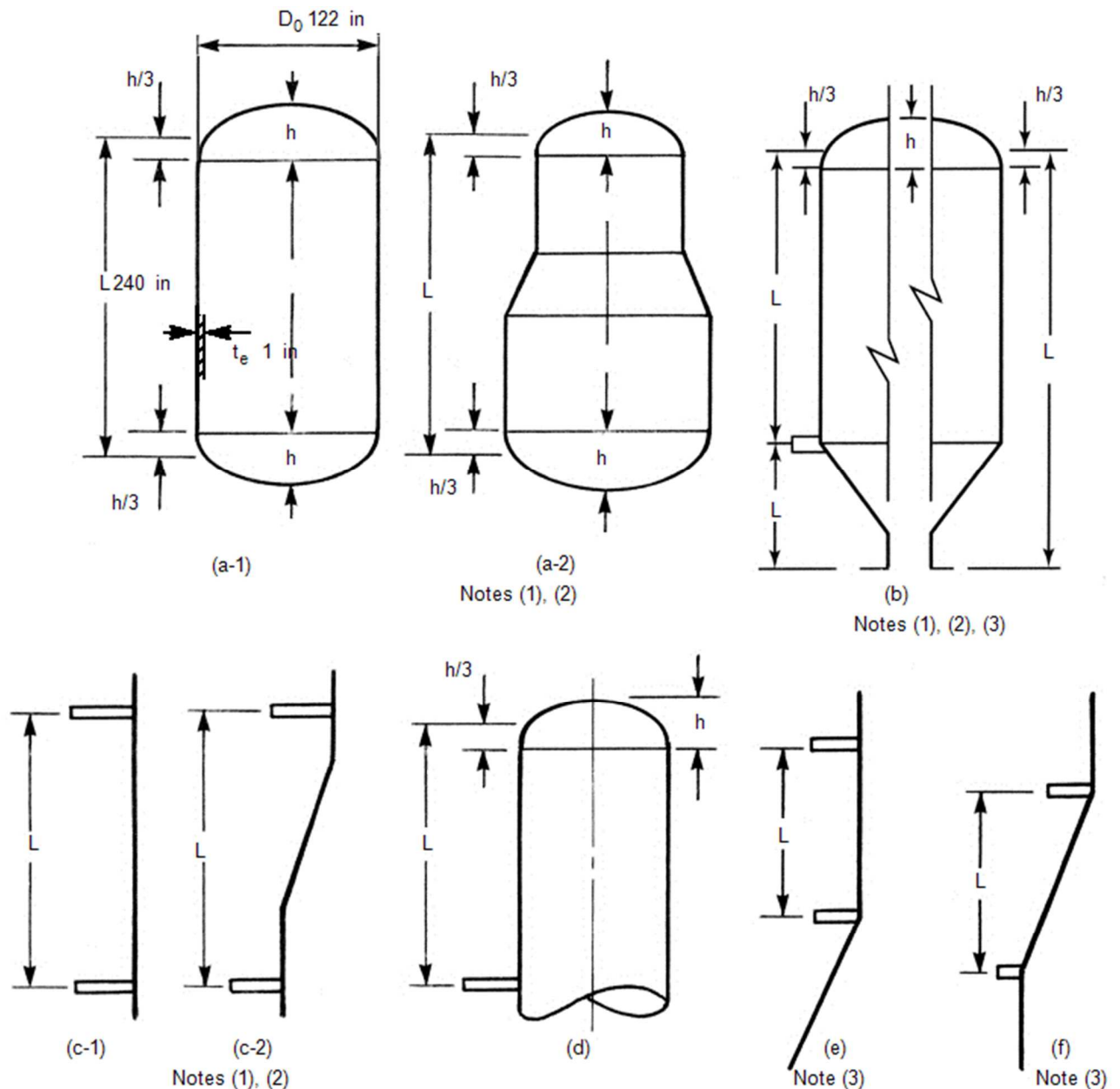
ASME BPVC VIII-1 2017
Example E4.4.7 - E4.4.8 PTB-4-2013

Thickness of shells and tubes under external pressure ASME BPVC VIII UG-28 and Appendix I, 2017 Edition

Cylindrical shells under external pressure

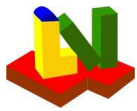
External design pressure
Hydrostatic head
External calculation pressure
Calculation temperature

p_D 14.7 psi
 D_p 0 psi
 p_0 14.7 psi
 T_0 300 °F



Outside diameter
Design wall thickness
Wall thickness allowance
Allowance (corrosion)
Buckling length

D_0 122 in
 t_e 1 in
 c_1 0 in
 c_2 0 in
 L 240 in



ASME BPVC VIII-1 2017

Example E4.4.7 - E4.4.8 PTB-4-2013

Material K02700-SA-516-70-Class:-Size:

Spec. Min. Yield	S_y	37710 psi
Allowable stress	S_0	20015 psi
Applicable material chart	Fig	CS-2
Modulus of elasticity	E	2.829e+7 psi

Results

Effective thickness	t_0	1 in
Ratio	L/D_0	1.967
Ratio	D_0/t_0	122
Factor according to ASME-IID\Table G	A	4.844e-4
Factor (see material chart)	B	6974 psi
Factor $2 \cdot \min(S_0; 9 \cdot B)$	S	12553 psi
Required thickness acc. UG-28	t_{UG-28}	13.22 mm
Required thickness acc. UG-16	t_{UG-16}	1.5 mm
Required thickness	t	0.5205 in
Required thickness incl. allowances	$t+c_1+c_2$	0.5205 in
Allowable excess pressure	P	74.89 psi
Allowable pressure without hydrostatic head	MAWP	74.89 psi

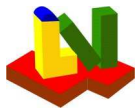
Remark

Equations

$$\frac{D_0}{t_0} \geq 10 \Leftrightarrow 122 \geq 10 \quad \text{UG-28 c) (1)}$$

$$Pa(B) = \frac{4 \cdot B}{3 \cdot \frac{D_0}{t_0}} = \frac{4 \cdot 48.08 \text{ N/mm}^2}{3 \cdot 122} = 0.5255 \text{ MPa} \quad \text{Step 6}$$

$$Pa(E) = \frac{2 \cdot A \cdot E}{3 \cdot \frac{D_0}{t_0}} = \frac{2 \cdot 4.844e-4 \cdot 195067 \text{ N/mm}^2}{3 \cdot 122} = 0.5163 \text{ MPa} \quad \text{Step 7}$$



ASME BPVC VIII-1 2017

Example E4.4.7 - E4.4.8 PTB-4-2013

Appendix: Material documentation

Section 2: Zylinder/UG33
Section 2: Kegel/UG33
Section 2: Versteifung/UG33
Section 3: Verstärkung/UG33
Section 4: Zylinder/UG33
Section 4: Kegel/UG33
Section 5: Verstärkung/UG33
Section 6: Boden/UG33
Section 7: Schale/UG28
Section 8: Boden/UG33
Section 9: Verstärkung/UG33
Section 10: Schale/UG28

Material specification:

Regulation: ASMET1A:2017Spec. No.: SA-516 Product: Plate
Material code: K02700-SA-516-70-Class:-Size: Short name: Carbon steel

Design conditions and dimensions:

Temperature [°C]: 148,8889 Pressure [bar]: 1,013536
Thickness [mm]: 46,04 Outside diameter [mm]: 3902,07

Material values for test and design conditions:

	Test condition	Operating condition
Nominal design strength [N/mm ²]:	138,00	138,00
Safety factor:	1,00	1,00
Allowable stress [N/mm ²]:	138,00	138,00
Modulus of elasticity [kN/mm ²]:	202	195,0667

Notes:

G10 General Requirements

Upon prolonged exposure to temperatures above 425°C, the carbide phase of carbon steel may be converted to graphite. See Nonmandatory Appendix A, A-201 and A-202.

S1 Size Requirements

For Section I applications, stress values at temperatures of 450°C and above are permissible but, except for tubular products 75 mm O.D. or less enclosed within the boiler setting, use of these materials at these temperatures is not current practice.

T2 Time-Dependent Properties

Allowable stresses for temperatures of 400°C and above are values obtained from time-dependent properties.

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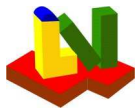
Creep rupture strength for 100000 h [MPa]:

Tensile strength and yield stress at ambient temperature:

Diam./.....	Tensile str....	ReH.....	Rupture.....	Rupture.....
Thick.....	Rm min.....	Rm max.....	elong.....	elong.....
<= mm.....	MPa.....	MPa.....	MPa.....	längs %.....	quer %.....
.....

K-values as function of the temperature

Diam./...
Thickn...	50°C.....	100°C.....	150°C.....	200°C.....	250°C.....	300°C.....	350°C.....	400°C.....
<= mm...	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
.....	138.....	138.....	138.....	138.....	136.....	128.....	101.....



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Example E4.4.7 - E4.4.8 PTB-4-2013

a K-values as function of the temperature

Diam./.....
Thickn.....	450°C.....	500°C.....	550°C.....	600°C.....	650°C.....	700°C.....	800°C.....
<= mm.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
.....	67.1.....	33.6.....	12.9.....

Modulus of elasticity in dependence of the temperature:

Static modulus of elasticity in [kN/mm²] at the temperature of

-75...	-200...	-125...	25...	100...	150...	200...	250...	300...	350...	400...	450...	500...	550...
209...	216...	212...	202...	198...	195...	192...	189...	185...	179...	171...	162...	151...	137...

Coefficient of linear expansion:

Thermal coefficient of expansion between 20°C and

Density	100°C..	200°C..	300°C..	400°C..	500°C..	600°C..	700°C..	800°C..	Heat...	Heat...
(20 °C)	cond...	capac...
kg/dm ³ ·	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	W/Km...	J/kgK...
7,85...	12,1...	12,7...	13,3...	13,8...	14,4...