

# ASME BPVC VIII-1 2017

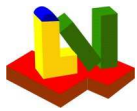
## Example E4.4.1 - E4.4.5 PTB-4-2013

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### Layout

Input values:	1.234	or	1.234
Calculated values:	<b>1.234</b>	or	<b>1.234</b>
Critical values:	<b>1.234</b>	or	<b>1.234</b>
Estimated values:	<b>1.234</b>	or	<b>1.234</b>



# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

### Comparison - Form for equations

#### Equation form

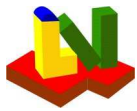
#### Comment

Results for example E4.4.1-5 acc. ASME and Lauterbach Verfahrenstechnik GmbH (LV)  
The LV-program uses formulas for thick cylinders acc. ASME VIII Div.1 UG28/33 and App.1.

#### Equations

#### Value

Conversion factor	$\text{mm}^2/\text{in} = 0.03937$	<b>0.03937</b>
.	$\text{MPa} \cdot 2\text{psi} = 145.037$	<b>145</b>
'Results Ex. E4.4.1 LV and ASME		<b>0</b>
Max.allowable Pressure P acc. LV	$P1 = \text{MPa} \cdot 2\text{psi} \cdot \#21(1)$	<b>39.03</b>
Max.allowable Pressure Pa acc. ASME	$P1\text{Asme} = 39$	<b>39</b>
Difference in %	$\text{Diff1} = (P1 - P1\text{Asme}) / P1\text{Asme} \cdot 100$	<b>0.06913</b>
'Results Ex. E4.4.2 LV and ASME		<b>0</b>
Max.allowable Pressure Pa acc. LV	$P2 = \text{MPa} \cdot 2\text{psi} \cdot \#29(9)$	<b>247.9</b>
Max.allowable Pressure Pa acc. ASME	$P2\text{Asme} = 249.6$	<b>249.6</b>
Difference in %	$\text{Diff2} = (P2 - P2\text{Asme}) / P2\text{Asme} \cdot 100$	<b>-0.6637</b>
'Results Ex. E4.4.3 LV and ASME with B taken by LV		<b>0</b>
Max.allowable Pressure P acc. LV	$P3a = \text{MPa} \cdot 2\text{psi} \cdot \#36(2)/10$	<b>582.5</b>
Max.allowable Pressure Pa acc. ASME	$P3a\text{Asme} = 571.1$	<b>571.1</b>
Difference in %	$\text{Diff3} = (P3a - P3a\text{Asme}) / P3a\text{Asme} \cdot 100$	<b>1.99</b>
'Results Ex. E4.4.3 LV and ASME with B =15700 (taken by ASME)		<b>0</b>
Max.allowable Pressure P acc. LV	$P3b = \text{MPa} \cdot 2\text{psi} \cdot \#36(3)/10$	<b>571.2</b>
Max.allowable Pressure Pa acc. ASME	$P3b\text{Asme} = 571.1$	<b>571.1</b>
Difference in %	$\text{Diff4} = (P3b - P3b\text{Asme}) / P3b\text{Asme} \cdot 100$	<b>0.02329</b>
'Results Ex. E4.4.4 LV and ASME with B taken by LV		<b>0</b>
Max.allowable Pressure P acc. LV	$P4 = \text{MPa} \cdot 2\text{psi} \cdot \#29(5)$	<b>55.72</b>
Max.allowable Pressure Pa acc. ASME	$P4\text{Asme} = 55.8$	<b>55.8</b>
Difference in %	$\text{Diff5} = (P4 - P4\text{Asme}) / P4\text{Asme} \cdot 100$	<b>-0.1501</b>
'Results Ex. E4.4.5 LV and ASME		<b>0</b>
Max.allowable Pressure P acc. LV	$P5 = \text{MPa} \cdot 2\text{psi} \cdot \#116(4)/10$	<b>166.2</b>
Max.allowable Pressure Pa acc. ASME	$P5\text{Asme} = 166.2$	<b>166.2</b>
Difference in %	$\text{Diff6} = (P5 - P5\text{Asme}) / P5\text{Asme} \cdot 100$	<b>-0.02726</b>
'Maximum difference between LV and ASME		<b>0</b>
$D_{\text{max}} = \text{Max}( \text{Diff1} ;  \text{Diff2} ;  \text{Diff3} ;  \text{Diff4} ;  \text{Diff5} ;  \text{Diff6} )$		<b>1.99</b>



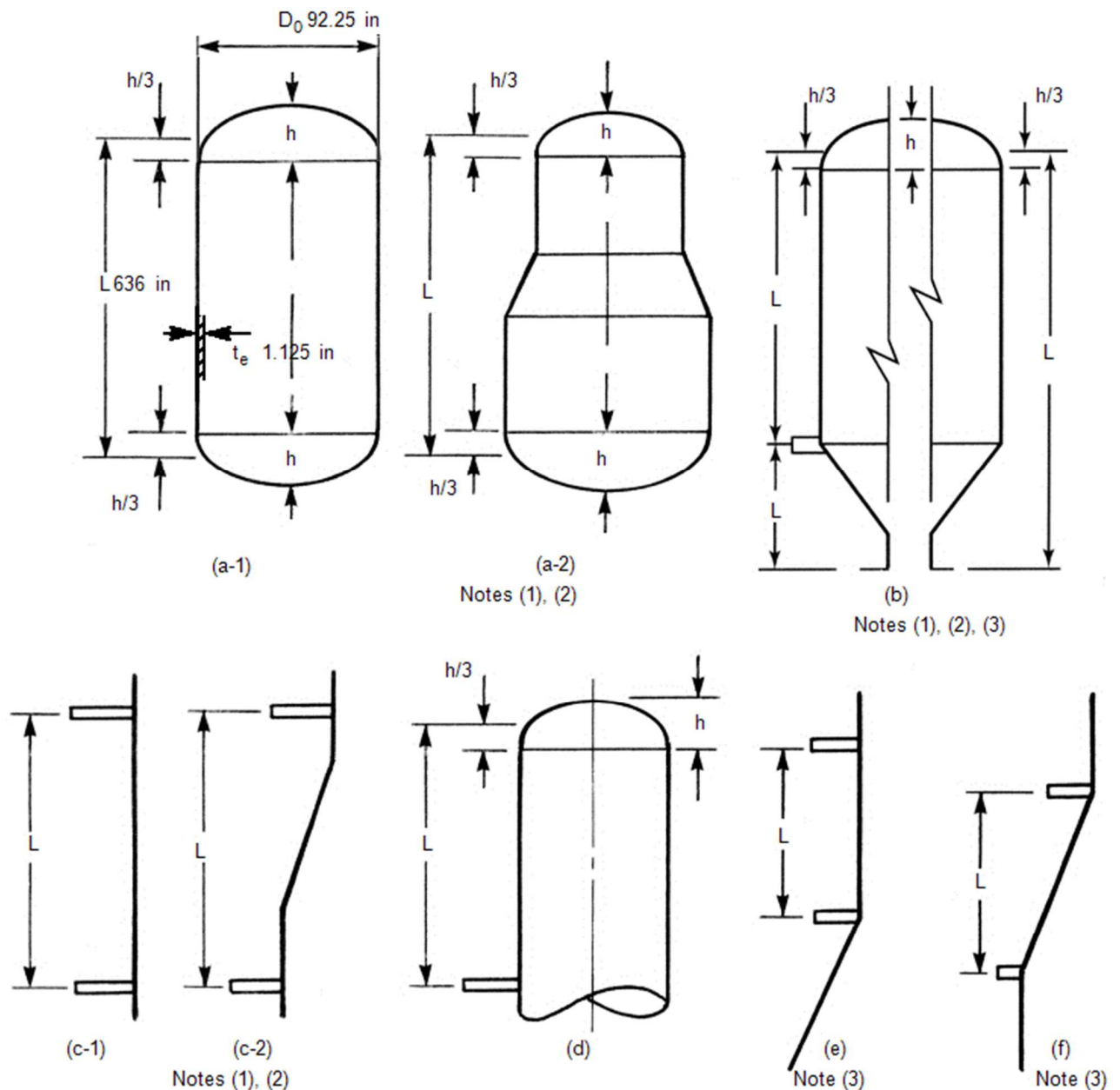
**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

**E4.4.1 - Thickness of shells and tubes under external pressure ASME BPVC VIII UG-28 and Appendix I, 2017 Edition**

**Cylindrical shells under external pressure**

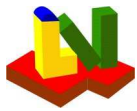
External design pressure  
Hydrostatic head  
External calculation pressure  
Calculation temperature

$p_D$  14.5 psi  
 $D_p$  0 psi  
 $p_0$  **14.5** psi  
 $T_0$  300 °F



Outside diameter  
Design wall thickness  
Wall thickness allowance  
Allowance (corrosion)  
Buckling length

$D_0$  92.25 in  
 $t_e$  1.125 in  
 $c_1$  0 in  
 $c_2$  0.125 in  
 $L$  636 in



# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

Material K02700-SA-516-70-Class:-Size:

Spec. Min. Yield	$S_y$	33600	psi
Allowable stress	$S_0$	20015	psi
Applicable material chart	Fig	CS-2	
Modulus of elasticity	E	2.829e+7	psi

### Results

Effective thickness	$t_0$	1	in
Ratio	$L/D_0$	6.894	
Ratio	$D_0/t_0$	92.25	
Factor according to ASME-IIID\Table G	A	1.884e-4	
Factor (see material chart)	B	2700	psi
Factor $2 \cdot \text{Min}(S_0; 9 \cdot B)$	S	4860	psi
Required thickness acc. UG-28	$t_{UG-28}$	17.06	mm
Required thickness acc. UG-16	$t_{UG-16}$	0.05906	in
Required thickness	t	0.6718	in
Required thickness incl. allowances	$t+c_1+c_2$	0.7968	in
Allowable excess pressure	P	38.51	psi
Allowable pressure without hydrostatic head	MAWP	38.51	psi

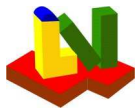
Remark

### Equations

$$\frac{D_0}{t_0} \geq 10 \Leftrightarrow 92.25 \geq 10 \quad \text{UG-28 c) (1)}$$

$$Pa(B) = \frac{4 \cdot B}{3 \cdot \frac{D_0}{t_0}} = \frac{4 \cdot 18.62 \text{ N/mm}^2}{3 \cdot 92.25} = 0.2691 \text{ MPa} \quad \text{Step 6}$$

$$Pa(E) = \frac{2 \cdot A \cdot E}{3 \cdot \frac{D_0}{t_0}} = \frac{2 \cdot 1.884e-4 \cdot 195054 \text{ N/mm}^2}{3 \cdot 92.25} = 0.2656 \text{ MPa} \quad \text{Step 7}$$



# **ASME BPVC VIII-1 2017** **Example E4.4.1 - E4.4.5 PTB-4-2013**

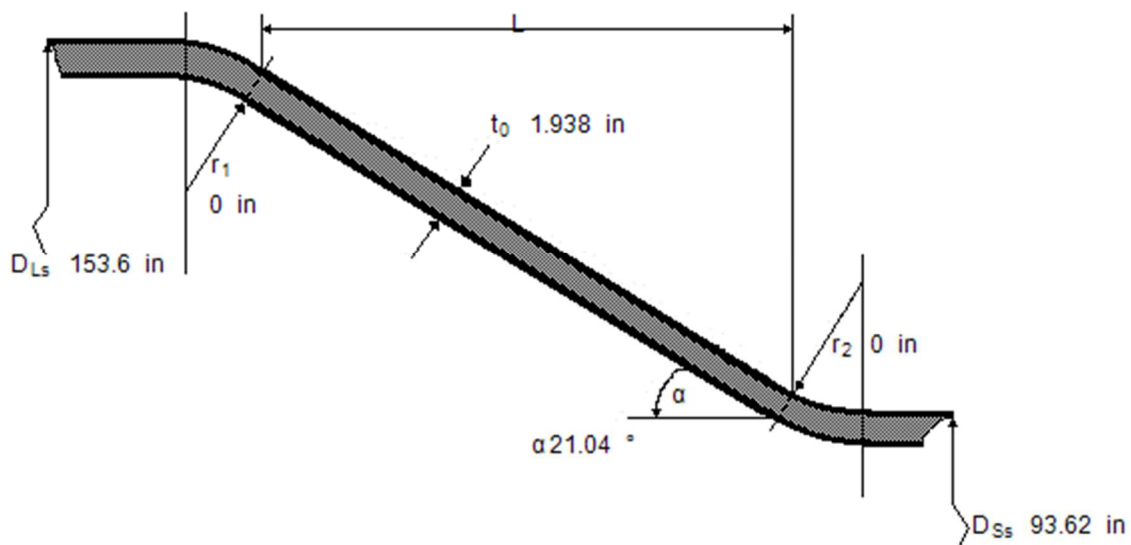
## **E4.4.2 with B taken by ASME - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition**

### **Conical shells under external pressure acc. UG-33(f)**

External design pressure	$p_D$	249 psi
Hydrostatic head	$D_p$	0 psi
Calculation pressure	$p_0$	249 psi
Calculation temperature	$T_0$	300 °F

Material K02700-SA-516-70-Class:-Size:

Spec. Min. Yield	$S_y$	33600 psi
Allowable stress	$S_0$	20015 psi
Applicable material chart	Fig	CS-2
E-Modulus	E	2.9e+7 psi

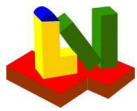


Cone wall thickness with allowances	$t_0$	1.938 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0.125 in
Cone wall thickness without allowances	$t$	1.813 in

Is a cylinder connected, which does not act as line of support?

	N	(Y/N)
Outside diameter (wide end)	$D_{Ls}$	153.6 in
Knuckle radius (wide end)	$r_1$	0 in
Outside diameter (small end)	$D_{Ss}$	93.62 in
Knuckle radius (small end)	$r_2$	0 in
Half apex angle ( $\leq 60^\circ$ )	$\alpha$	21.04 °

**Proof for cross-section area according to App. 1-8 required for cone-connection without knuckle**



# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

### Results

Effective thickness	$t_e = t \cdot \cos(\alpha)$	$t_e$	1.692 in
Axial length of the cone		L	78 in
Design length		$L_e$	62.77 in
Ratio		$L_e/D_L$	0.4086
Ratio		$D_L/t_e$	90.81
Factor according to fig. 5-UGO-28.0		A	0.004132
Factor (see material chart)		B	17000 psi
Factor	$2 \cdot \min(S_0; 9 \cdot B)$	S	31589 psi
Allowable external pressure (for $t_0$ )		P	249.6 psi
Allowable pressure without hydrostatic head		MEP	249.6 psi
Required thickness (for $P_0$ )		t	1.819 in
Required thickness incl. allowances		$t+c_1+c_2$	1.944 in

Remark **Thickness not sufficient**

### Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$D_L = D_{Ls} - r_1 \cdot (1 - \cos(\alpha)) = 3902 \text{ mm} - 0 \text{ mm} \cdot (1 - 0.9333) = 3902 \text{ mm}$$

$$D_S = D_{Ss} + r_2 \cdot (1 - \cos(\alpha)) = 2378 \text{ mm} + 0 \text{ mm} \cdot (1 - 0.9333) = 2378 \text{ mm}$$

$$L = \frac{(D_L - D_S)}{2} \cdot \tan(\alpha) = \frac{(3902 \text{ mm} - 2378 \text{ mm})}{2} \cdot 0.3846 = 1981 \text{ mm}$$

$$L_1 = r_1 \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.359 = 0 \text{ mm}$$

$$L_2 = r_2 \cdot \left( \frac{D_{Ss}}{D_{Ls}} \right) \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.6094 \cdot 0.359 = 0 \text{ mm}$$

$$L_3 = \frac{L}{2} \cdot \frac{(D_L + D_S)}{D_{Ls}} = \frac{1981 \text{ mm}}{2} \cdot \frac{(3902 \text{ mm} + 2378 \text{ mm})}{3902 \text{ mm}} = 1594 \text{ mm}$$

$$L_e = L_1 + L_2 + L_3 = 0 \text{ mm} + 0 \text{ mm} + 1594 \text{ mm} = 1594 \text{ mm}$$

1) for  $D_L/t_0 \geq 10$

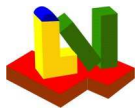
$$Pa(B) = \frac{4 \cdot B}{3 \cdot \left( \frac{D_L}{t_0} \right)} = \frac{4 \cdot 117.2 \text{ N/mm}^2}{3 \cdot 90.81} = 1.721 \text{ N/mm}^2$$

UG-33 f-a) Step 6

$$Pa(E) = \frac{2 \cdot A \cdot E}{3 \cdot \left( \frac{D_L}{t_0} \right)} = \frac{2 \cdot 0.004132 \cdot 199948 \text{ N/mm}^2}{3 \cdot 90.81} = 6.066 \text{ N/mm}^2$$

UG-33 f-a) Step 7

2) for  $D_L/t_0 < 10$



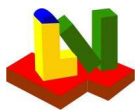
**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

$$P_{a1} = \left[ \frac{2.167}{\frac{D_L}{t_0}} - 0.0833 \right] \cdot B = \left[ \frac{2.167}{90.81} - 0.0833 \right] \cdot 117.2 \text{ N/mm}^2 = -6.967 \text{ N/mm}^2$$

UG-33 f-b) Step 2

$$P_{a2} = \frac{2 \cdot S}{\frac{D_L}{t_0}} \cdot \left[ 1 - \frac{2 \cdot S}{\frac{D_L}{t_0}} \right] = \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \cdot \left[ 1 - \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \right] = 4.744 \text{ N/mm}^2$$

UG-33 f-b) Step 3



**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

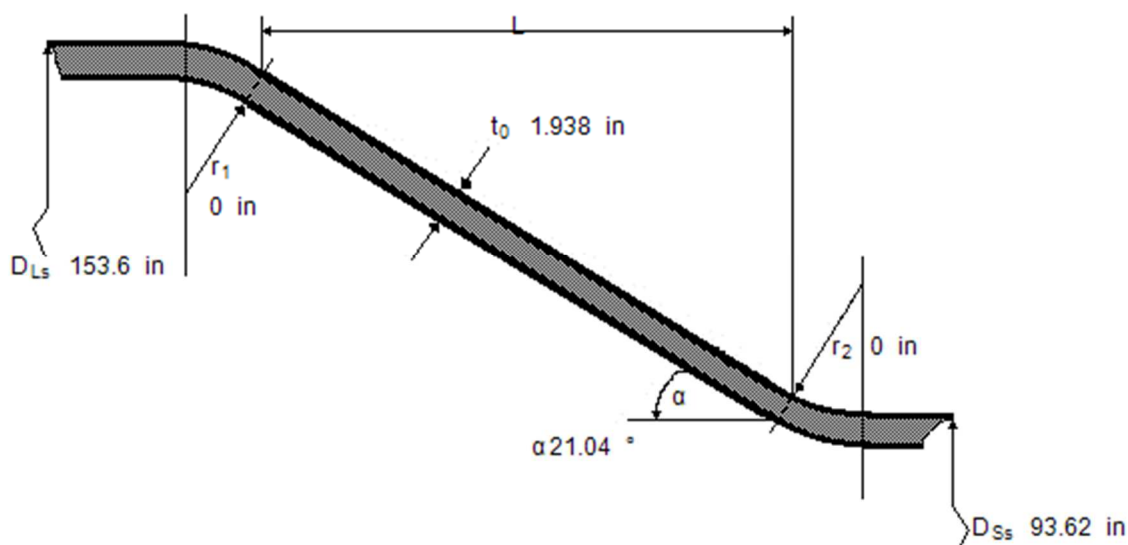
**E4.4.2 with B taken by LV - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition**

**Conical shells under external pressure acc. UG-33(f)**

External design pressure	$p_D$	249 psi
Hydrostatic head	$D_p$	0 psi
Calculation pressure	$p_0$	249 psi
Calculation temperature	$T_0$	300 °F

Material K02700-SA-516-70-Class:-Size:

Spec. Min. Yield	$S_y$	33600 psi
Allowable stress	$S_0$	20015 psi
Applicable material chart	Fig	CS-2
E-Modulus	E	2.9e+7 psi



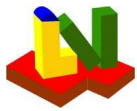
Cone wall thickness with allowances	$t_0$	1.938 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0.125 in
Cone wall thickness without allowances	$t$	1.813 in

Is a cylinder connected, which does not act as line of support?

	N	(Y/N)
Outside diameter (wide end)	$D_{Ls}$	153.6 in
Knuckle radius (wide end)	$r_1$	0 in
Outside diameter (small end)	$D_{Ss}$	93.62 in
Knuckle radius (small end)	$r_2$	0 in
Half apex angle ( $\leq 60^\circ$ )	$\alpha$	21.04 °

**Proof for cross-section area according to App. 1-8 required for cone-connection without knuckle**





# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

### Results

Effective thickness	$t_e = t \cdot \cos(\alpha)$	$t_e$	<b>1.692</b> in
Axial length of the cone		$L$	<b>78</b> in
Design length		$L_e$	<b>62.77</b> in
Ratio		$L_e/D_L$	<b>0.4086</b>
Ratio		$D_L/t_e$	<b>90.81</b>
Factor according to fig. 5-UGO-28.0		$A$	<b>0.004132</b>
Factor (see material chart)		$B$	<b>16887</b> psi
Factor	$2 \cdot \min(S_0; 9 \cdot B)$	$S$	<b>31589</b> psi
Allowable external pressure (for $t_0$ )		$P$	<b>247.9</b> psi
Allowable pressure without hydrostatic head		MEP	<b>247.9</b> psi
Required thickness (for $P_0$ )		$t$	<b>1.819</b> in
Required thickness incl. allowances		$t+c_1+c_2$	<b>1.944</b> in

Remark **Pressure not allowable**

### Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$D_L = D_{Ls} - r_1 \cdot (1 - \cos(\alpha)) = 3902 \text{ mm} - 0 \text{ mm} \cdot (1 - 0.9333) = 3902 \text{ mm}$$

$$D_S = D_{Ss} + r_2 \cdot (1 - \cos(\alpha)) = 2378 \text{ mm} + 0 \text{ mm} \cdot (1 - 0.9333) = 2378 \text{ mm}$$

$$L = \frac{(D_L - D_S)}{2} \cdot \tan(\alpha) = \frac{(3902 \text{ mm} - 2378 \text{ mm})}{2} \cdot 0.3846 = 1981 \text{ mm}$$

$$L_1 = r_1 \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.359 = 0 \text{ mm}$$

$$L_2 = r_2 \cdot \left( \frac{D_{Ss}}{D_{Ls}} \right) \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.6094 \cdot 0.359 = 0 \text{ mm}$$

$$L_3 = \frac{L}{2} \cdot \frac{(D_L + D_S)}{D_{Ls}} = \frac{1981 \text{ mm}}{2} \cdot \frac{(3902 \text{ mm} + 2378 \text{ mm})}{3902 \text{ mm}} = 1594 \text{ mm}$$

$$L_e = L_1 + L_2 + L_3 = 0 \text{ mm} + 0 \text{ mm} + 1594 \text{ mm} = 1594 \text{ mm}$$

1) for  $D_L/t_0 \geq 10$

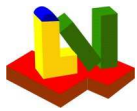
$$Pa(B) = \frac{4 \cdot B}{3 \cdot \left( \frac{D_L}{t_0} \right)} = \frac{4 \cdot 116.4 \text{ N/mm}^2}{3 \cdot 90.81} = 1.71 \text{ N/mm}^2$$

UG-33 f-a) Step 6

$$Pa(E) = \frac{2 \cdot A \cdot E}{3 \cdot \left( \frac{D_L}{t_0} \right)} = \frac{2 \cdot 0.004132 \cdot 199948 \text{ N/mm}^2}{3 \cdot 90.81} = 6.066 \text{ N/mm}^2$$

UG-33 f-a) Step 7

2) for  $D_L/t_0 < 10$



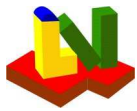
**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

$$P_{a1} = \left[ \frac{2.167}{\frac{D_L}{t_0}} - 0.0833 \right] \cdot B = \left[ \frac{2.167}{90.81} - 0.0833 \right] \cdot 116.4 \text{ N/mm}^2 = -6.92 \text{ N/mm}^2$$

UG-33 f-b) Step 2

$$P_{a2} = \frac{2 \cdot S}{\frac{D_L}{t_0}} \cdot \left[ 1 - \frac{2 \cdot S}{\frac{D_L}{t_0}} \right] = \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \cdot \left[ 1 - \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \right] = 4.744 \text{ N/mm}^2$$

UG-33 f-b) Step 3



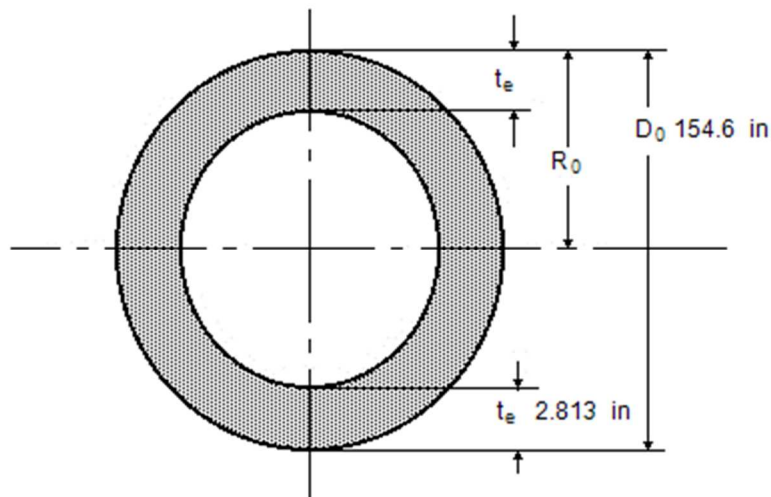
**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

**E4.4.3 with B taken by LV - Thickness of shells and tubes under external pressure ASME BPVC VIII UG-28 and Appendix I, 2017 Edition**

**Spherical shells under external pressure**

External design pressure  
Hydrostatic head  
External calculation pressure  
Calculation temperature

$p_D$  572 psi  
 $D_p$  0 psi  
 $p_0$  **572** psi  
 $T_0$  350 °F



Outside diameter  
Design wall thickness  
Wall thickness allowance  
Allowance (corrosion)

$D_0$  154.6 in  
 $t_e$  2.813 in  
 $c_1$  0 in  
 $c_2$  0 in

Material K31835-SA-542-D-Class:4a-Size:

Spec. Min. Yield  
Allowable stress  
Applicable material chart  
Modulus of elasticity

$S_y$  60190 psi  
 $S_0$  24366 psi  
Fig CS-2  
 $E$  2.852e+7 psi

**Results**

Effective thickness  
Tip radius  
Ratio

$t_0$  **2.813** in  
 $R_0$  **77.3** in  
 $R_0/t_0$  **27.48**

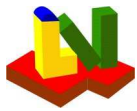
Factor  $0.125/(R_0/t_0)$   
Factor (see material chart)

A **0.004548**  
B **16009** psi

Required thickness acc. UG-28  
Required thickness acc. UG-16  
Required thickness  
Required thickness incl. allowances  
Allowable excess pressure  
Allowable pressure without hydrostatic head

$t_{UG-28}$  **70.29** mm  
 $t_{UG-16}$  0.05906 in  
 $t$  **2.767** in  
 $t+c_1+c_2$  **2.767** in  
P **582.5** psi  
MAWP **582.5** psi

Remark



**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

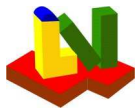
**Equations**

$$Pa(B) = \frac{B}{\left(\frac{R_0}{t_0}\right)} = \frac{110.4 \text{ N/mm}^2}{27.48} = 4.016 \text{ MPa}$$

UG-28 d)    Step 4

$$Pa(E) = 0.0625 \cdot \frac{E}{\left(\frac{R_0}{t_0}\right)^2} = 0.0625 \cdot \frac{196606 \text{ N/mm}^2}{(27.48)^2} = 16.27 \text{ MPa}$$

UG-28 d)    Step 5



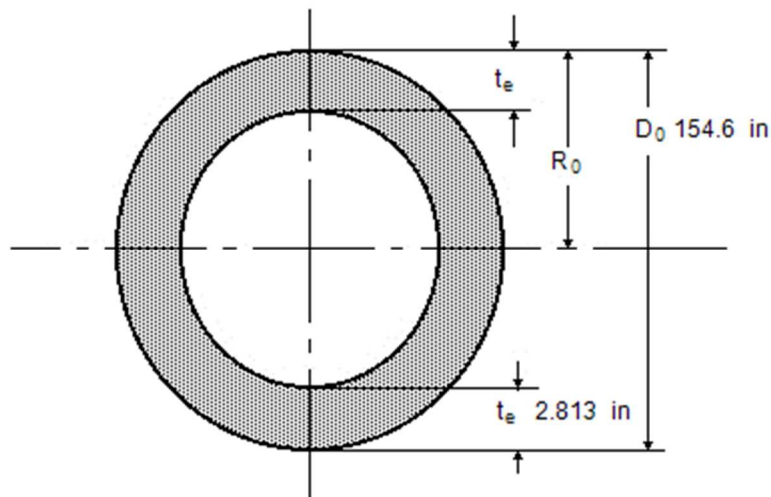
**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

**E4.4.3 with B taken by ASME - Thickness of shells and tubes under external pressure ASME BPVC VIII UG-28 and Appendix I, 2017 Edition**

**Spherical shells under external pressure**

External design pressure  
Hydrostatic head  
External calculation pressure  
Calculation temperature

$p_D$  571.1 psi  
 $D_p$  0 psi  
 $p_0$  **571.1** psi  
 $T_0$  350 °F



Outside diameter  
Design wall thickness  
Wall thickness allowance  
Allowance (corrosion)

$D_0$  154.6 in  
 $t_e$  2.813 in  
 $c_1$  0 in  
 $c_2$  0 in

Material K31835-SA-542-D-Class:4a-Size:

Spec. Min. Yield  
Allowable stress  
Applicable material chart  
Modulus of elasticity

$S_y$  60190 psi  
 $S_0$  24366 psi  
Fig CS-2  
 $E$  2.852e+7 psi

**Results**

Effective thickness  
Tip radius  
Ratio

$t_0$  **2.813** in  
 $R_0$  **77.3** in  
 $R_0/t_0$  **27.48**

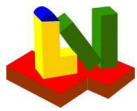
Factor  $0.125/(R_0/t_0)$   
Factor (see material chart)

A **0.004548**  
B 15700 psi

Required thickness acc. UG-28  
Required thickness acc. UG-16  
Required thickness  
Required thickness incl. allowances  
Allowable excess pressure  
Allowable pressure without hydrostatic head

$t_{UG-28}$  **70.19** mm  
 $t_{UG-16}$  0.05906 in  
 $t$  **2.763** in  
 $t+c_1+c_2$  **2.763** in  
P **571.2** psi  
MAWP **571.2** psi

Remark



**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

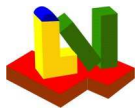
**Equations**

$$Pa(B) = \frac{B}{\left(\frac{R_0}{t_0}\right)} = \frac{108.2 \text{ N/mm}^2}{27.48} = 3.939 \text{ MPa}$$

UG-28 d) Step 4

$$Pa(E) = 0.0625 \cdot \frac{E}{\left(\frac{R_0}{t_0}\right)^2} = 0.0625 \cdot \frac{196606 \text{ N/mm}^2}{(27.48)^2} = 16.27 \text{ MPa}$$

UG-28 d) Step 5

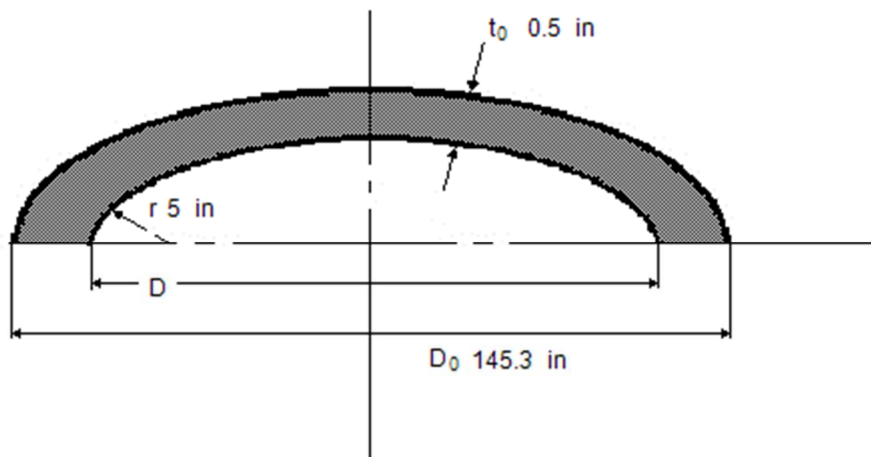


**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

**E4.4.4 with B taken by LV - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition**

**Torispherical heads**

External design pressure	$p_D$	55.6 psi
Hydrostatic head	$D_p$	0 psi
Calculation pressure	$p_0$	<b>55.6</b> psi
Calculation temperature	$T_0$	650 °F
Design wall thickness	$t_e$	0.625 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0.125 in
Effective thickness	$t_0$	<b>0.5</b> in



Outside diameter of the head skirt	$D_0$	145.3 in
Type of head	Torispherical head	
Outside calotte radius	$R_0$	72.63 in
Knuckle radius	$r$	5 in

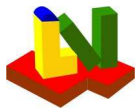
Material K11789-SA-387-11-Class:1-Size:

Spec. Min. Yield	$S_y$	34809 psi
Allowable stress	$S_0$	17114 psi
Applicable material chart	Fig	CS-2
Modulus of elasticity	$E$	2.512e+7 psi

**Results**

Ratio	$R_0/t_0$	<b>145.3</b>
Factor (see material chart)	$B$	<b>8093</b> psi
Allowable external pressure	$P$	<b>55.72</b> psi
Allowable pressure without hydrostatic head	MEP	<b>55.72</b> psi
Required thickness	$t$	0.499 in
Required thickness incl. allowances	$t+c_1+c_2$	0.624 in

Remark



**ASME BPVC VIII-1 2017**  
Example E4.4.1 - E4.4.5 PTB-4-2013

**Equations**

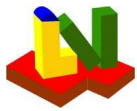
$$Pa(B) = \frac{B}{\left(R_0/t_0\right)} = \frac{55.8 \text{ N/mm}^2}{145.3} = 0.3842 \text{ N/mm}^2$$

UG-28 d) Step 4

$$Pa(E) = 0.0625 \cdot \frac{E}{\left(R_0/t_0\right)^2} = 0.0625 \cdot \frac{173231 \text{ N/mm}^2}{(145.3)^2} = 0.5131 \text{ N/mm}^2$$

UG-28 d) Step 5





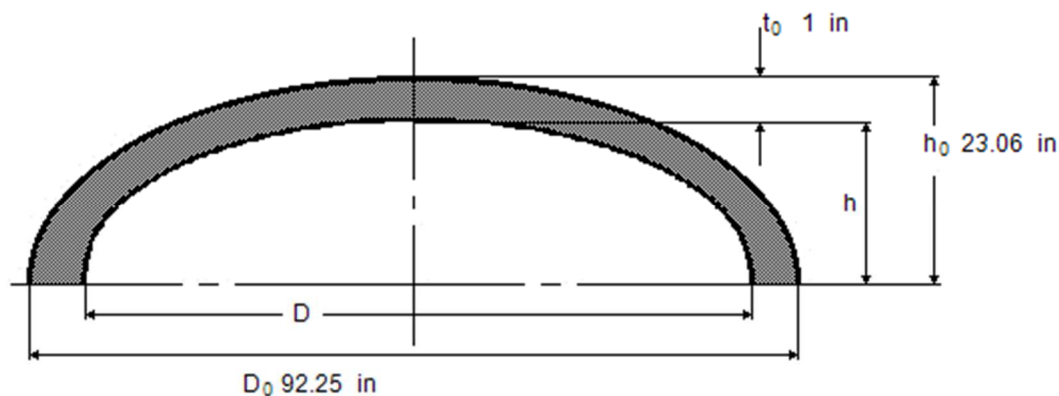
# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

### E4.4.5 - Formed heads pressure on convex side ASME BPVC VIII UG-33 and APP. 1, 2017 Edition

#### Ellipsoidal heads under external pressure

External design pressure	$p_D$	166.1 psi
Hydrostatic head	$D_p$	0 psi
Calculation pressure	$p_0$	166.1 psi
Calculation temperature	$T_0$	300 °F
Final wall thickness	$t_e$	1.125 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0.125 in
Effective thickness	$t_0$	1 in



Outside diameter of the head skirt	$D_0$	92.25 in
Outer height of crown (short semiaxis)	$h_0$	23.06 in

Material K02700-SA-516-70-Class:-Size:

Spec. Min. Yield	$S_y$	37710 psi
Allowable stress	$S_0$	20015 psi
Applicable material chart	Fig	CS-2
E-Modulus	$E$	2.9e+7 psi

#### Results

Ratio	$D_0/2h_0$	2
Factor (according to chart UG-33.1)	$K_0$	0.9
Design radius of crown	$R_0$	83.02 in
Ratio	$R_0/t_0$	83.02
Factor	$A$	0.001506
Factor (see material chart)	$B$	13795 psi
Allowable external pressure	$P$	166.2 psi
Allowable pressure without hydrostatic head	MEP	166.2 psi
Required thickness without allowance	$t$	0.9999 in
Required thickness incl. allowances	$t+c_1+c_2$	1.125 in

Remark

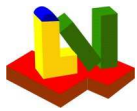
#### Equations

$$Pa(B) = \frac{B}{\left(R_0/t_0\right)} = \frac{95.11 \text{ N/mm}^2}{83.02} = 1.146 \text{ N/mm}^2$$

UG-28 d) Step 4

$$Pa(E) = 0.0625 \cdot \frac{E}{\left(R_0/t_0\right)^2} = 0.0625 \cdot \frac{199948 \text{ N/mm}^2}{(83.02)^2} = 1.813 \text{ N/mm}^2$$

UG-28 d) Step 5



# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

### Appendix: Material documentation

Section 2: Schale/UG28  
Section 3: Boden/UG33  
Section 4: Boden/UG33

#### Material specification:

Regulation: ASME1A:2017Spec. No.: SA-516 Product: Plate  
Material code: K02700-SA-516-70-Class:-Size: Short name: Carbon steel

#### Design conditions and dimensions:

Temperature [°C]: 148,8889 Pressure [bar]: 1  
Thickness [mm]: 28,575 Outside diameter [mm]: 2343,15

#### Material values for test and design conditions:

	Test condition	Operating condition
Nominal design strength [N/mm <sup>2</sup> ]:	138,00	138,00
Safety factor:	1,00	1,00
Allowable stress [N/mm <sup>2</sup> ]:	138,00	138,00
Modulus of elasticity [kN/mm <sup>2</sup> ]:	202	195,0667

#### Notes:

G10 General Requirements

Upon prolonged exposure to temperatures above 425°C, the carbide phase of carbon steel may be converted to graphite. See Nonmandatory Appendix A, A-201 and A-202.

#### S1 Size Requirements

For Section I applications, stress values at temperatures of 450°C and above are permissible but, except for tubular products 75 mm O.D. or less enclosed within the boiler setting, use of these materials at these temperatures is not current practice.

#### T2 Time-Dependent Properties

Allowable stresses for temperatures of 400°C and above are values obtained from time-dependent properties.

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Creep rupture strength for 100000 h [MPa]:

#### Tensile strength and yield stress at ambient temperature:

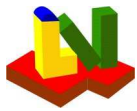
Diam./.....	Tensile str....	.....	ReH.....	Rupture.....	Rupture.....
Thickn.....	Rm min.....	Rm max.....	.....	elong.....	elong.....
<= mm.....	MPa.....	MPa.....	MPa.....	längs %.....	quer %.....
.....	.....	.....	.....	.....	.....

K-values as function of the temperature

Diam./...	.....	.....	.....	.....	.....	.....	.....	.....
Thickn...	50°C.....	100°C.....	150°C.....	200°C.....	250°C.....	300°C.....	350°C.....	400°C.....
<= mm...	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
.....	.....	138.....	138.....	138.....	138.....	136.....	128.....	101.....

K-values as function of the temperature

Diam./.....	.....	.....	.....	.....	.....	.....	.....	.....
Thickn.....	450°C.....	500°C.....	550°C.....	600°C.....	650°C.....	700°C.....	800°C.....	.....
<= mm.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	.....
.....	67.1.....	33.6.....	12.9.....	.....	.....	.....	.....	.....



# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

### Modulus of elasticity in dependence of the temperature:

Static modulus of elasticity in [kN/mm<sup>2</sup>] at the temperature of

-75...	-200...	-125...	25...	100...	150...	200...	250...	300...	350...	400...	450...	500...	550...
209...	216...	212...	202...	198...	195...	192...	189...	185...	179...	171...	162...	151...	137...

### Coefficient of linear expansion:

Thermal coefficient of expansion between 20°C and

Density (20 °C)	100°C..	200°C..	300°C..	400°C..	500°C..	600°C..	700°C..	800°C..	Heat...	Heat...
kg/dm <sup>3</sup>	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	W/Km...	J/kgK...
7,85...	12,1...	12,7...	13,3...	13,8...	14,4...	...	...	...	...	...

Section 5: Schale/UG28

### Material specification:

Regulation: ASMET1A:2017Spec. No.: SA-542 Product: Plate  
Material code: K31835-SA-542-D-Class:4a-Size: Short name: 2.25Cr-1Mo-V

### Design conditions and dimensions:

Temperature [°C]: 176,67 Pressure [bar]: 39,44  
Thickness [mm]: 71,44 Outside diameter [mm]: 3926,84

### Material values for test and design conditions:

	Test condition	Operating condition
Nominal design strength [N/mm <sup>2</sup> ]:	168,00	168,00
Safety factor:	1,00	1,00
Allowable stress [N/mm <sup>2</sup> ]:	168,00	168,00
Modulus of elasticity [kN/mm <sup>2</sup> ]:	200	196,6056

### Notes:

--  
Creep rupture strength for 100000 h [MPa]:

### Tensile strength and yield stress at ambient temperature:

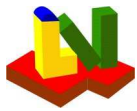
Diam./...	Tensile str...	ReH.....	Rupture.....	Rupture.....
Thickn....	Rm min.....	Rm max.....	elong.....	elong.....
<= mm.....	MPa.....	MPa.....	längs %.....	quer %.....
.....	.....	.....	.....	.....

K-values as function of the temperature

Diam./...	.....	.....	.....	.....	.....	.....	.....	.....
Thickn....	50°C.....	100°C.....	150°C.....	200°C.....	250°C.....	300°C.....	350°C.....	400°C.....
<= mm.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
.....	.....	168.....	168.....	168.....	168.....	165.....	159.....	153.....

K-values as function of the temperature

Diam./...	.....	.....	.....	.....	.....	.....	.....	.....
Thickn....	450°C.....	500°C.....	550°C.....	600°C.....	650°C.....	700°C.....	800°C.....	.....
<= mm.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	.....
.....	145.....	137.....	.....	.....	.....	.....	.....	.....



# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

### Modulus of elasticity in dependence of the temperature:

Static modulus of elasticity in [kN/mm<sup>2</sup>] at the temperature of

260.....	370.....	480.....	425.....	20.....	150.....
-----	-----	-----	-----	-----	-----
186.....	169.....	143.....	157.....	200.....	200.....

### Coefficient of linear expansion:

Thermal coefficient of expansion between 20°C and

Density (20 °C)	100°C..	200°C..	300°C..	400°C..	500°C..	600°C..	700°C..	800°C..	Heat...	Heat...
kg/dm <sup>3</sup>	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	W/Km...	J/kgK...
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
.....	12,1...	12,7...	13,3...	13,8...	14,4...	.....	.....	.....	.....	.....

Section 6: Schale/UG28

### Material specification:

Regulation: ASMET1A:2017Spec. No.: SA-542 Product: Plate  
Material code: K31835-SA-542-D-Class:4a-Size: Short name: 2.25Cr-1Mo-V

### Design conditions and dimensions:

Temperature [°C]: 176,6667 Pressure [bar]: 39,38  
Thickness [mm]: 71,4375 Outside diameter [mm]: 3926,84

### Material values for test and design conditions:

	Test condition	Operating condition
Nominal design strength [N/mm <sup>2</sup> ]:	168,00	168,00
Safety factor:	1,00	1,00
Allowable stress [N/mm <sup>2</sup> ]:	168,00	168,00
Modulus of elasticity [kN/mm <sup>2</sup> ]:	200	196,606

### Notes:

--  
Creep rupture strength for 100000 h [MPa]:

### Tensile strength and yield stress at ambient temperature:

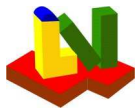
Diam./.....	Tensile str....	.....	ReH.....	Rupture.....	Rupture.....
Thickn.....	Rm min.....	Rm max.....	.....	elong.....	elong.....
<= mm.....	MPa.....	MPa.....	MPa.....	längs %.....	quer %.....
-----	-----	-----	-----	-----	-----
.....	.....	.....	.....	.....	.....

K-values as function of the temperature

Diam./...	.....	.....	.....	.....	.....	.....	.....	.....
Thickn...	50°C.....	100°C.....	150°C.....	200°C.....	250°C.....	300°C.....	350°C.....	400°C.....
<= mm...	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
-----	-----	-----	-----	-----	-----	-----	-----	-----
.....	.....	168.....	168.....	168.....	168.....	165.....	159.....	153.....

K-values as function of the temperature

Diam./.....	.....	.....	.....	.....	.....	.....	.....
Thickn....	450°C.....	500°C.....	550°C.....	600°C.....	650°C.....	700°C.....	800°C.....
<= mm.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
-----	-----	-----	-----	-----	-----	-----	-----
.....	145.....	137.....	.....	.....	.....	.....	.....



# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

### Modulus of elasticity in dependence of the temperature:

Static modulus of elasticity in [kN/mm<sup>2</sup>] at the temperature of

260.....	370.....	480.....	425.....	20.....	150.....
-----	-----	-----	-----	-----	-----
186.....	169.....	143.....	157.....	200.....	200.....

### Coefficient of linear expansion:

Thermal coefficient of expansion between 20°C and

Density (20 °C)	100°C..	200°C..	300°C..	400°C..	500°C..	600°C..	700°C..	800°C..	Heat...	Heat...
kg/dm <sup>3</sup>	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	W/Km...	J/kgK...
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
.....	12,1...	12,7...	13,3...	13,8...	14,4...	.....	.....	.....	.....	.....

Section 7: Boden/UG33

### Material specification:

Regulation: ASMET1A:2017Spec. No.: SA-387 Product: Plate  
Material code: K11789-SA-387-11-Class:1-Size: Short name: 1.25Cr-0.5Mo-Si

### Design conditions and dimensions:

Temperature [°C]: 343,33 Pressure [bar]: 3,83  
Thickness [mm]: 15,88 Outside diameter [mm]: 3690,62

### Material values for test and design conditions:

	Test condition	Operating condition
Nominal design strength [N/mm <sup>2</sup> ]:	118,00	118,00
Safety factor:	1,00	1,00
Allowable stress [N/mm <sup>2</sup> ]:	118,00	118,00
Modulus of elasticity [kN/mm <sup>2</sup> ]:	204	183,4002

Notes:

S4 Size Requirements

For Section I applications, stress values at temperatures of 625°C and above are permissible but, except for tubular products 75 mm O.D. or less enclosed within the boiler setting, use of these materials at these temperatures is not current practice.

T4 Time-Dependent Properties

Allowable stresses for temperatures of 480°C and above are values obtained from time-dependent properties.

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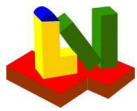
Creep rupture strength for 100000 h [MPa]:

### Tensile strength and yield stress at ambient temperature:

Diam./.....	Tensile str....	.....	ReH.....	Rupture.....	Rupture.....
Thick.....	Rm min.....	Rm max.....	.....	elong.....	elong.....
<= mm.....	MPa.....	MPa.....	MPa.....	längs %.....	quer %.....
-----	-----	-----	-----	-----	-----
.....	.....	.....	.....	.....	.....

K-values as function of the temperature

Diam./...	.....	.....	.....	.....	.....	.....	.....	.....
Thickn...	50°C.....	100°C.....	150°C.....	200°C.....	250°C.....	300°C.....	350°C.....	400°C.....
<= mm...	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
-----	-----	-----	-----	-----	-----	-----	-----	-----
.....	.....	118.....	118.....	118.....	118.....	118.....	118.....	118.....



# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

K-values as function of the temperature

Diam./.....	.....	.....	.....	.....	.....	.....	.....
Thickn.....	450°C.....	500°C.....	550°C.....	600°C.....	650°C.....	700°C.....	800°C.....
<= mm.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
.....	114.....	74.7.....	36.5.....	17.6.....	8.08.....	.....	.....

### Modulus of elasticity in dependence of the temperature:

Static modulus of elasticity in [kN/mm<sup>2</sup>] at the temperature of

650..	-75..	-200..	-125..	25..	100..	150..	200..	250..	300..	350..	400..	450..	500..	550..
150..	210..	218..	213..	204..	200..	197..	193..	190..	186..	183..	179..	174..	169..	164..

Static modulus of elasticity in [kN/mm<sup>2</sup>] at the temperature of

600.....	700.....	.....	.....	.....
157.....	142.....	.....	.....	.....

### Coefficient of linear expansion:

Thermal coefficient of expansion between 20°C and

Density	100°C..	200°C..	300°C..	400°C..	500°C..	600°C..	700°C..	800°C..	Heat...	Heat...
(20 °C)	.....	.....	.....	.....	.....	.....	.....	.....	cond...	capac...
kg/dm <sup>3</sup> ·	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	W/Km...	J/kgK...
7,85...	12,1...	12,7...	13,3...	13,8...	14,4...	.....	.....	.....	.....	.....

Section 8: Boden/UG33

### Material specification:

Regulation:	ASMET1A:2017Spec. No.:	SA-516	Product:	Plate
Material code:	K02700-SA-516-70-Class:-Size:		Short name:	Carbon steel

### Design conditions and dimensions:

Temperature [°C]:	148,89	Pressure [bar]:	11,45
Thickness [mm]:	28,58	Outside diameter [mm]:	2343,15

### Material values for test and design conditions:

	Test condition	Operating condition
Nominal design strength [N/mm <sup>2</sup> ]:	138,00	138,00
Safety factor:	1,00	1,00
Allowable stress [N/mm <sup>2</sup> ]:	138,00	138,00
Modulus of elasticity [kN/mm <sup>2</sup> ]:	202	195,0666

Notes:

G10 General Requirements

Upon prolonged exposure to temperatures above 425°C, the carbide phase of carbon steel may be converted to graphite. See Nonmandatory Appendix A, A-201 and A-202.

S1 Size Requirements

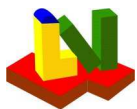
For Section I applications, stress values at temperatures of 450°C and above are permissible but, except for tubular products 75 mm O.D. or less enclosed within the boiler setting, use of these materials at these temperatures is not current practice.

T2 Time-Dependent Properties

Allowable stresses for temperatures of 400°C and above are values obtained from time-dependent properties.

--

Creep rupture strength for 100000 h [MPa]:



# ASME BPVC VIII-1 2017

## Example E4.4.1 - E4.4.5 PTB-4-2013

### Tensile strength and yield stress at ambient temperature:

Diam./.....	Tensile str....	.....	ReH.....	Rupture.....	Rupture.....
Thick.....	Rm min.....	Rm max.....	.....	elong.....	elong.....
<= mm.....	MPa.....	MPa.....	MPa.....	lāngs %.....	quer %.....
-----	-----	-----	-----	-----	-----
.....	.....	.....	.....	.....	.....

K-values as function of the temperature

Diam./...	.....	.....	.....	.....	.....	.....	.....	.....
Thickn...	50°C.....	100°C.....	150°C.....	200°C.....	250°C.....	300°C.....	350°C.....	400°C.....
<= mm...	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
-----	-----	-----	-----	-----	-----	-----	-----	-----
.....	.....	138.....	138.....	138.....	138.....	136.....	128.....	101.....

K-values as function of the temperature

Diam./.....	.....	.....	.....	.....	.....	.....	.....	.....
Thickn....	450°C.....	500°C.....	550°C.....	600°C.....	650°C.....	700°C.....	800°C.....	.....
<= mm.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....	MPa.....
-----	-----	-----	-----	-----	-----	-----	-----	-----
.....	67.1.....	33.6.....	12.9.....	.....	.....	.....	.....	.....

### Modulus of elasticity in dependence of the temperature:

Static modulus of elasticity in [kN/mm<sup>2</sup>] at the temperature of

-75...	-200...	-125...	25...	100...	150...	200...	250...	300...	350...	400...	450...	500...	550...
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
209...	216...	212...	202...	198...	195...	192...	189...	185...	179...	171...	162...	151...	137...

### Coefficient of linear expansion:

Thermal coefficient of expansion between 20°C and

Density	100°C..	200°C..	300°C..	400°C..	500°C..	600°C..	700°C..	800°C..	Heat...	Heat...
(20 °C)	.....	.....	.....	.....	.....	.....	.....	.....	cond...	capac..
kg/dm³·	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	10E-6/K	W/Km...	J/kgK..
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
7,85...	12,1...	12,7...	13,3...	13,8...	14,4...	.....	.....	.....	.....	.....